

## Using Stata with Multiple Regression & Matrices

1. **Matrix calculations with Stata.** Stata has several built-in functions that make it work as a matrix calculator. These functions are probably primarily helpful to programmers who want to write their own routines.

To get the M matrix, you can use the `mat accum` command. The `mat accum` command adds  $X_0$  to the list of variables (where  $X_0 = 1$  for all cases) and then computes all cross-products.

```
. mat accum m = income educ jobexp
(obs=20)

. mat list m

symmetric m[4,4]
      income      educ      jobexp      _cons
income 13742.27
      educ    6588.3    3285
jobexp  6448.9    2999    3767
_cons   488.3     241     253     20
```

To get the XP matrix of cross-product deviations from the means, we add the `dev` and `noconstant` parameters. The `dev` parameter subtracts the mean of the variable from each case while `noconstant` keeps  $X_0$  from being added to the data.

```
. mat accum xp = income educ jobexp, dev noconstant
(obs=20)

. mat list xp

symmetric xp[3,3]
      income      educ      jobexp
income 1820.4255
      educ    704.28499    380.95
jobexp  271.90499    -49.65    566.55
```

The covariance matrix can now be computed from the xp matrix. The sample size used when computing the xp matrix is stored by Stata in a scalar called `r(N)`.

```
. mat s = xp/(r(N)-1)

. mat list s

symmetric s[3,3]
      income      educ      jobexp
income 95.811867
      educ    37.067631    20.05
jobexp  14.310789    -2.6131579    29.818421
```

The `corr` function can be used to compute the correlations of the variables. The correlations can be computed from either the xp or covariance matrix.

```

. mat r = corr(s)

. mat list r

symmetric r[3,3]
      income      educ      jobexp
income      1
educ      .84572271      1
jobexp      .26773898      -.10687254      1

```

It wouldn't be as much fun, but you can just use the `corr` program to get the covariances and correlations. To get the correlations,

```

. corr income educ jobexp
(obs=20)

-----+-----
      | income      educ      jobexp
-----+-----
income | 1.0000
educ   | 0.8457      1.0000
jobexp | 0.2677     -0.1069      1.0000

```

To get the covariances instead, use the `cov` parameter.

```

. corr income educ jobexp, cov
(obs=20)

-----+-----
      | income      educ      jobexp
-----+-----
income | 95.8119
educ   | 37.0676      20.05
jobexp | 14.3108     -2.61316     29.8184

```

2. Do it yourself regression. Want to double-check Stata's regression estimates? You can do it with Stata's matrix commands. Recall that  $b = (X'X)^{-1}X'Y$ . In words, we say  $b$  equals  $X$  prime  $X$  inverse  $X$  prime  $Y$ .  $X'X$  is the cross-product matrix of the  $X$ 's with each other, including  $X_0$ . To compute it in Stata,

```

. mat accum xprimex = educ jobexp
(obs=20)

. mat list xprimex

symmetric xprimex[3,3]
      educ      jobexp      _cons
educ      3285
jobexp      2999      3767
_cons      241      253      20

```

$X'Y$  is the cross-product of  $Y$  with each of the  $X$ 's. `mat vecaccum` will compute  $Y'X$  for us. It computes the cross-product of the first variable listed with all the other variables listed.

```
. mat vecaccum yprimex = income educ jobexp
```

```
. mat list yprimex
```

```
yprimex[1,3]
      educ  jobexp  _cons
income 6588.3 6448.9 488.3
```

Note that this is a row vector. To get  $X'Y$ , which is a column vector, we simply transpose  $Y'X$ .

```
. mat xprimey = yprimex'
```

```
. mat list xprimey
```

```
xprimey[3,1]
      income
educ 6588.3
jobexp 6448.9
_cons 488.3
```

Now we are ready for the final calculation!

```
. mat b = inv(xprimex)*xprimey
```

```
. mat list b
```

```
b[3,1]
      income
educ 1.9333928
jobexp .64936536
_cons -7.0968549
```

3. [Optional] Proof that  $b = (X'X)^{-1}X'Y$ . Let  $X$  be an  $N \times K$  matrix (i.e.  $N$  cases, each of which has  $K$   $X$  variables, including  $X_0$ .)  $Y$  is an  $N \times 1$  matrix.  $e$  is an  $N \times 1$  matrix. Then, if the assumptions of OLS regression are met,

$Y = Xb + e$	
$Y - e = Xb$	Subtract $e$ from both sides
$X'(Y - e) = X'Xb$	Premultiply both sides by $X'$
$X'Y = X'Xb$	If the assumptions of OLS regression are met, $X'e = 0$ because the $X$ s are uncorrelated with the residuals of $Y$
$(X'X)^{-1}X'Y = (X'X)^{-1}X'Xb$	Premultiply both sides by $(X'X)^{-1}$
$(X'X)^{-1}X'Y = b$	$(X'X)^{-1}X'X = I$ and $Ib = b$