

# Verification and Validation of Scientific and Economic Simulations

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# Overview

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## □ Introduction

- Concepts of Verification and Validation
- Research Objectives and Methods

## □ Case Studies

- An Agent-based Scientific Model
- An Equation-based Economic Model

## □ Conclusion

## □ Future Work

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# Model Verification & Validation (V & V)

## □ V & V

### ■ Verification:

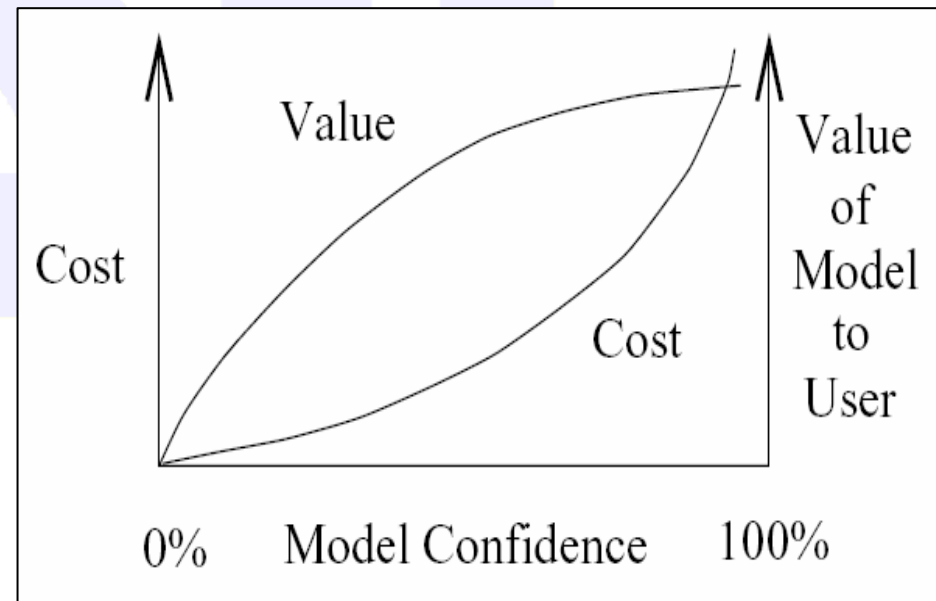
□ *get model right*

### ■ Validation:

□ *get right model*

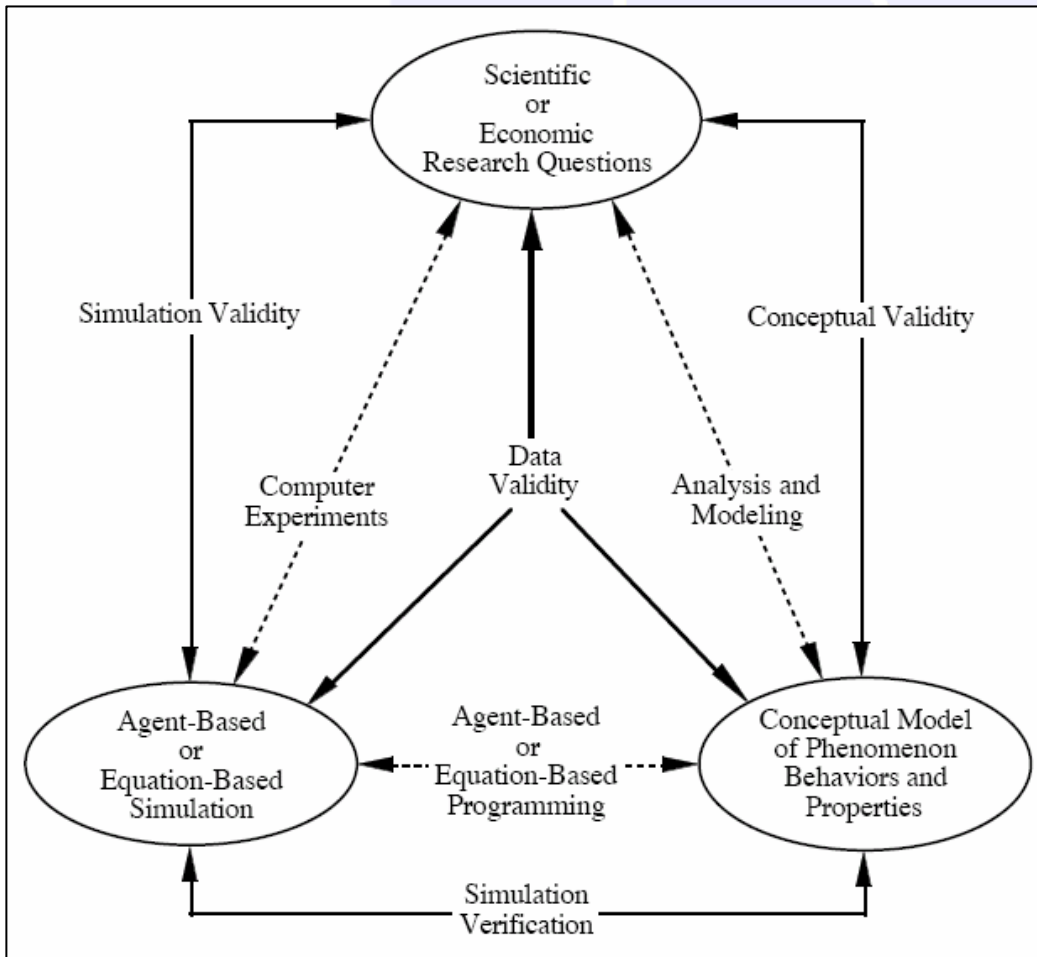
□ The cost and value influence confidence of model

□ Want to utilize V & V for optimal cost-effectiveness



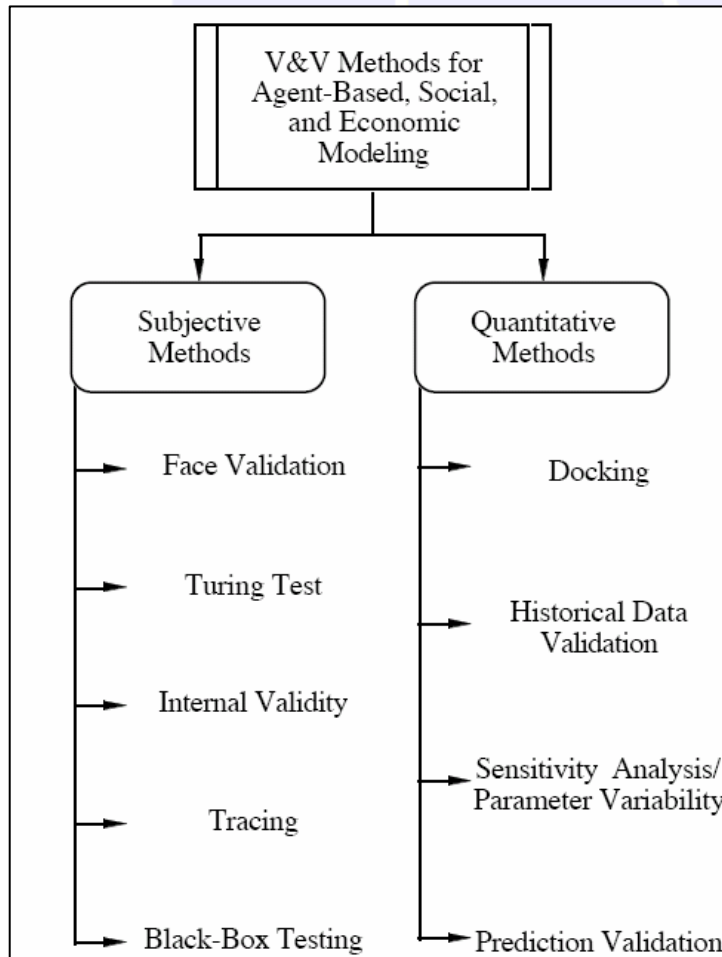
\*Adapted from Sargent: "Verification and Validation of Simulation Models"

# Verification and Validation Process



\*Adapted from Sargent: "Verification and Validation of Simulation Models" and Huang: "Agent-Based Scientific Simulation"

# Applicable Verification and Validation Methods



\*Balci: "Handbook of Simulation: Principles, Methodology, Advances, Applications, and Practice" lists more than 75 Methods

# V & V: Subjective Analysis

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## □ Examples of V & V Techniques

### ■ Face Validity

#### □ Animation

#### □ Graphical Representation

### ■ Turing Test

### ■ Internal Validity

### ■ Tracing

### ■ Black-Box Testing

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# V & V: Quantitative Analysis

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## □ Examples of V & V Techniques

- Model-to-Model Comparison (Docking)
- Historical Data Validation
- Sensitivity Analysis/Parameter Variability
- Prediction Validation

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# What and How

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## □ Research objective

- Perform V & V on distinct models and identify the more cost-effective techniques

## □ How

- Two very different projects as case studies
- Evaluate and adapt the formalized V & V techniques in industrial and system engineering

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# Case Study 1:

## An Agent-based Scientific Model

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- NSF funded interdisciplinary project
  - Understanding the evolution and heterogeneous structure of Natural Organic Matter (NOM)
  - E-science example
  - Chemists, biologists, ecologists, and computer scientists
- Agent-based stochastic model
- Web-based simulation model

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# Case Study 1:

## NOM

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### □ What is NOM?

- Heterogeneous mixture of molecules in terrestrial and aquatic ecosystems

### □ Why study NOM?

- Plays a crucial role in the evolution of soils, the transport of pollutants, and the global carbon cycle
- Understanding NOM helps us better understand natural ecosystems

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# Case Study 1:

## The Conceptual Model I

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### □ Agents

#### ■ A large number of molecules

##### □ Heterogeneous properties

- Elemental composition
- Molecular weight
- Characteristic functional groups

#### ■ Behaviors

##### □ Transport through soil pores (spatial mobility)

##### □ Chemical reactions: first order and second order

##### □ Sorption

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# Case Study 1:

## The Conceptual Model II

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### □ Stochastic Model

- Individual behaviors and interactions are stochastically determined by:

- Internal attributes

- Molecular structure
- State (adsorbed, desorbed, reacted, etc.)

- External conditions

- Environment (pH, light intensity, etc.)
- Proximity to other molecules

- Length of time step,  $\Delta t$

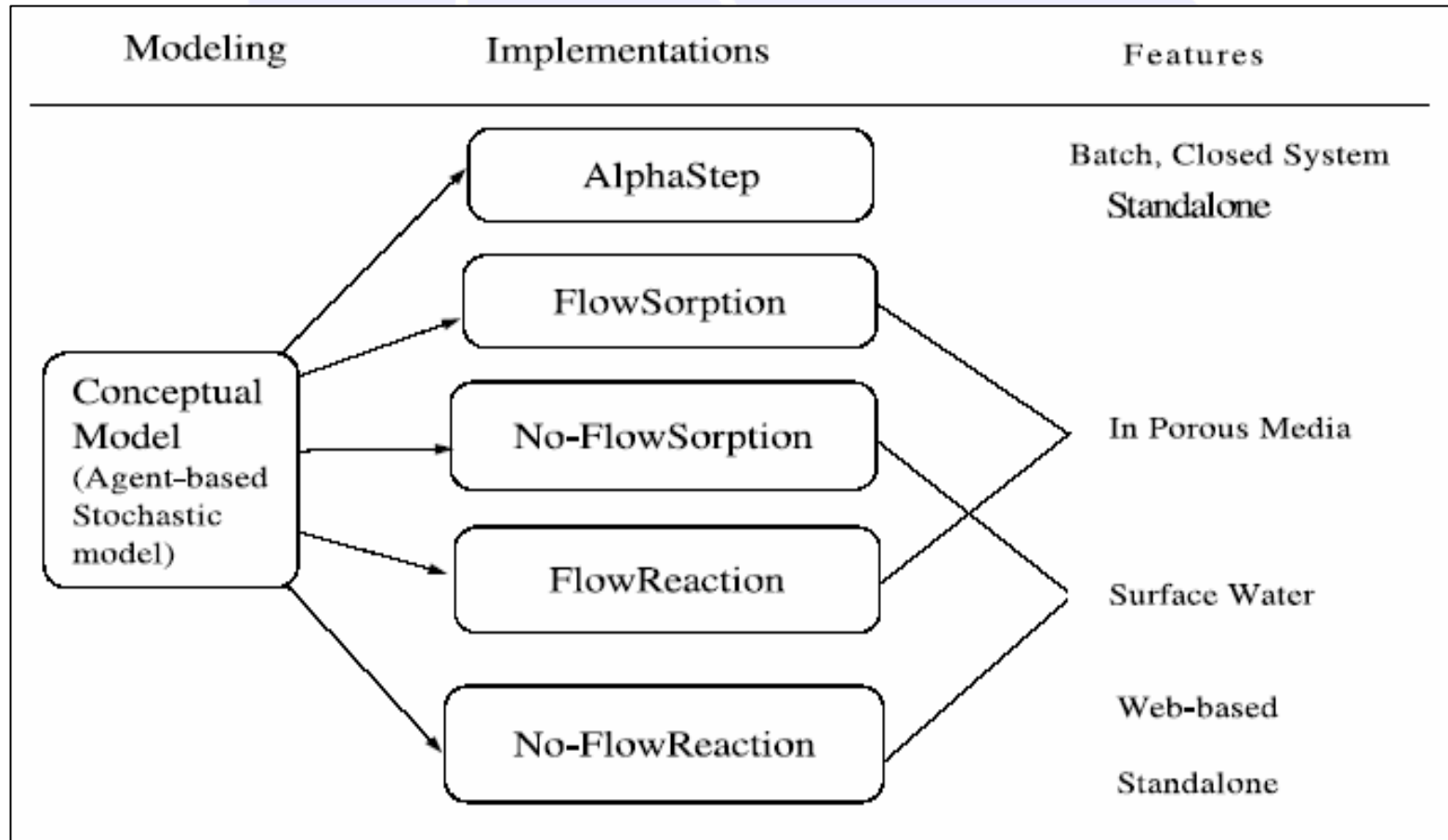
### □ Space

- 2D Grid Structure

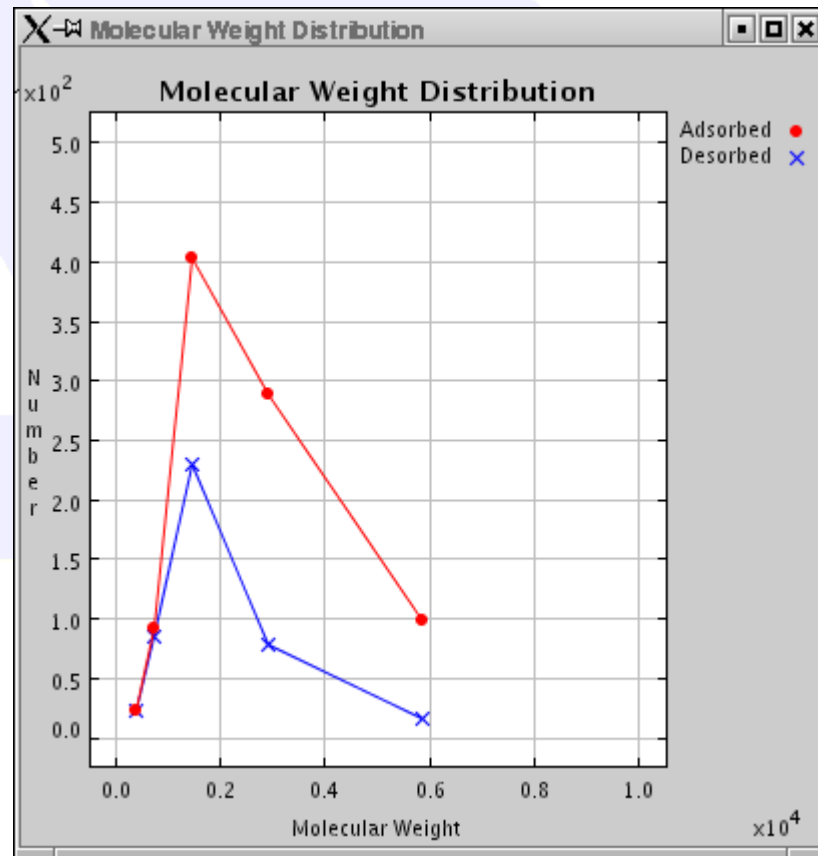
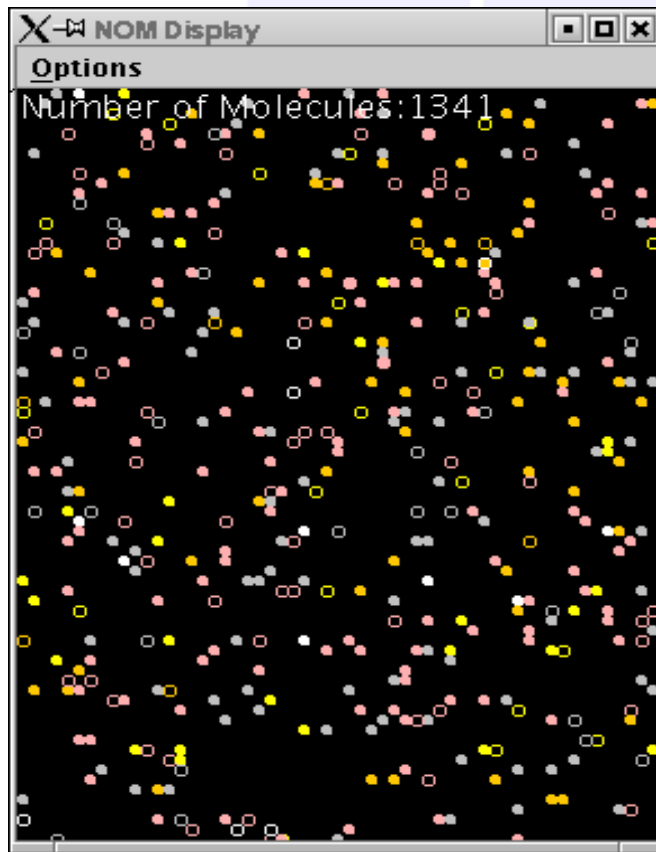
### □ Emergent properties

- Distribution of molecular properties over time

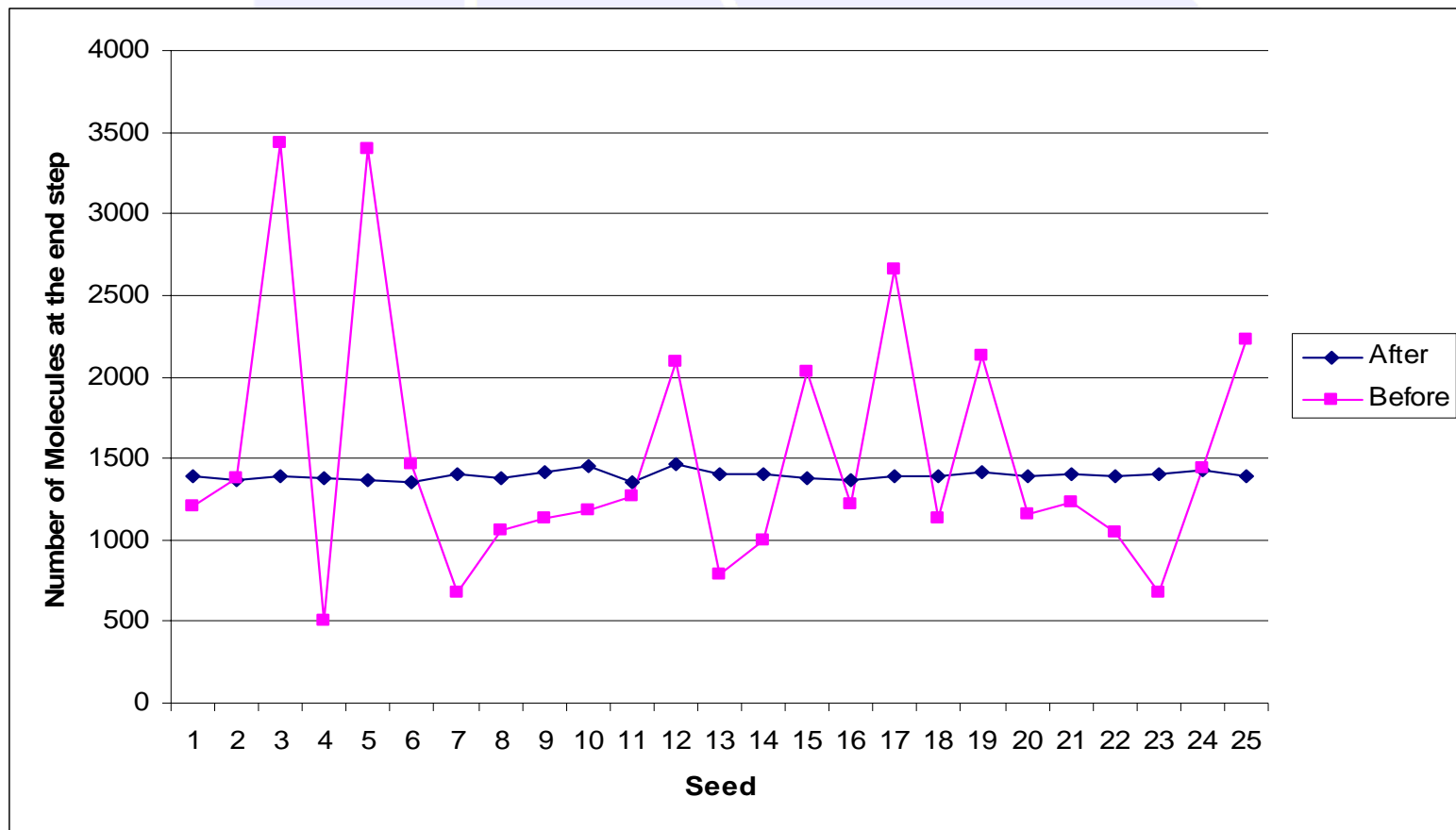
# Case Study 1: Implementations



# Case Study 1: Face Validity

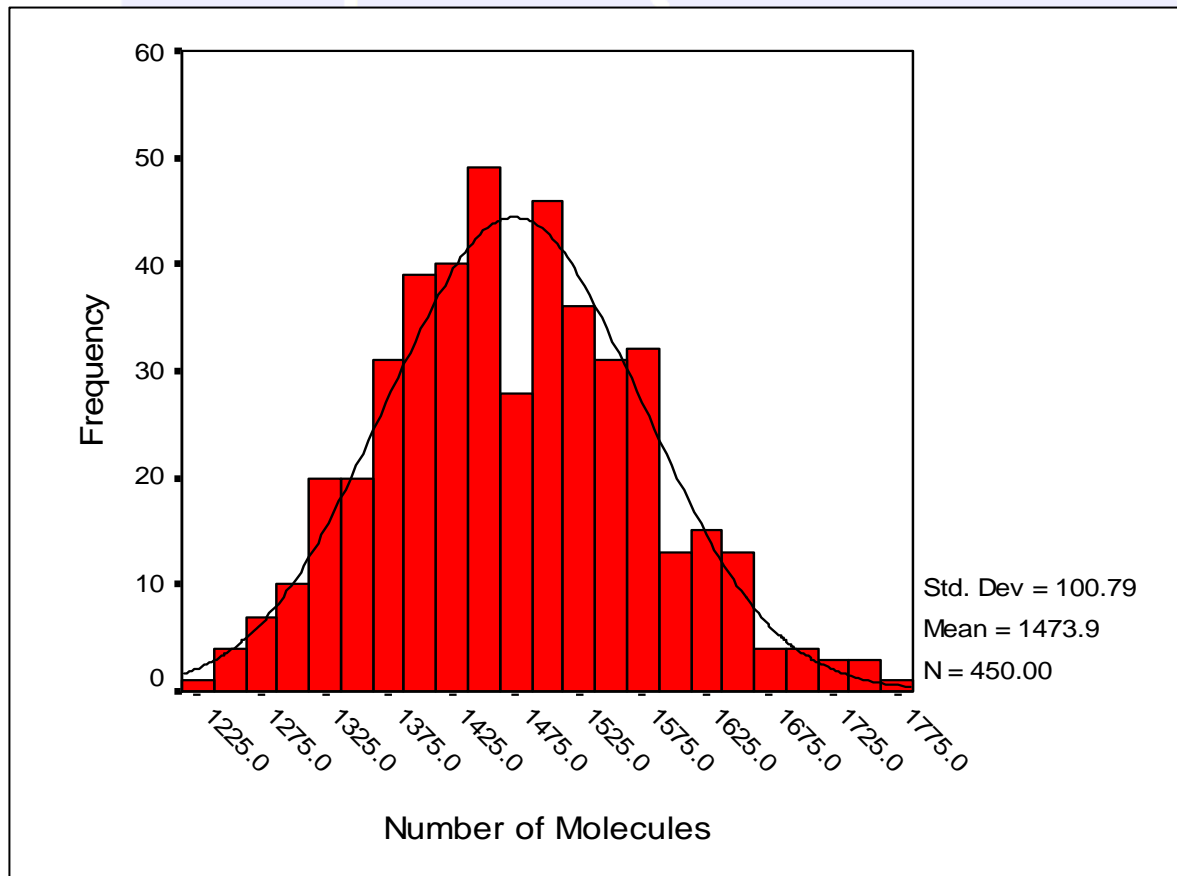


# Case Study 1: Internal Validity I



# Case Study 1: Internal Validity II

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# Case Study 1:

## Model-to-Model Comparison I

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- ❑ Compare the model with validated one
- ❑ Compare the model with non-validated one
- ❑ Different implementations
  - Different programming languages
  - Different packages
- ❑ Different modeling approaches
  - Agent-based approach vs. Equation-based approach
- ❑ Powerful method for ABS

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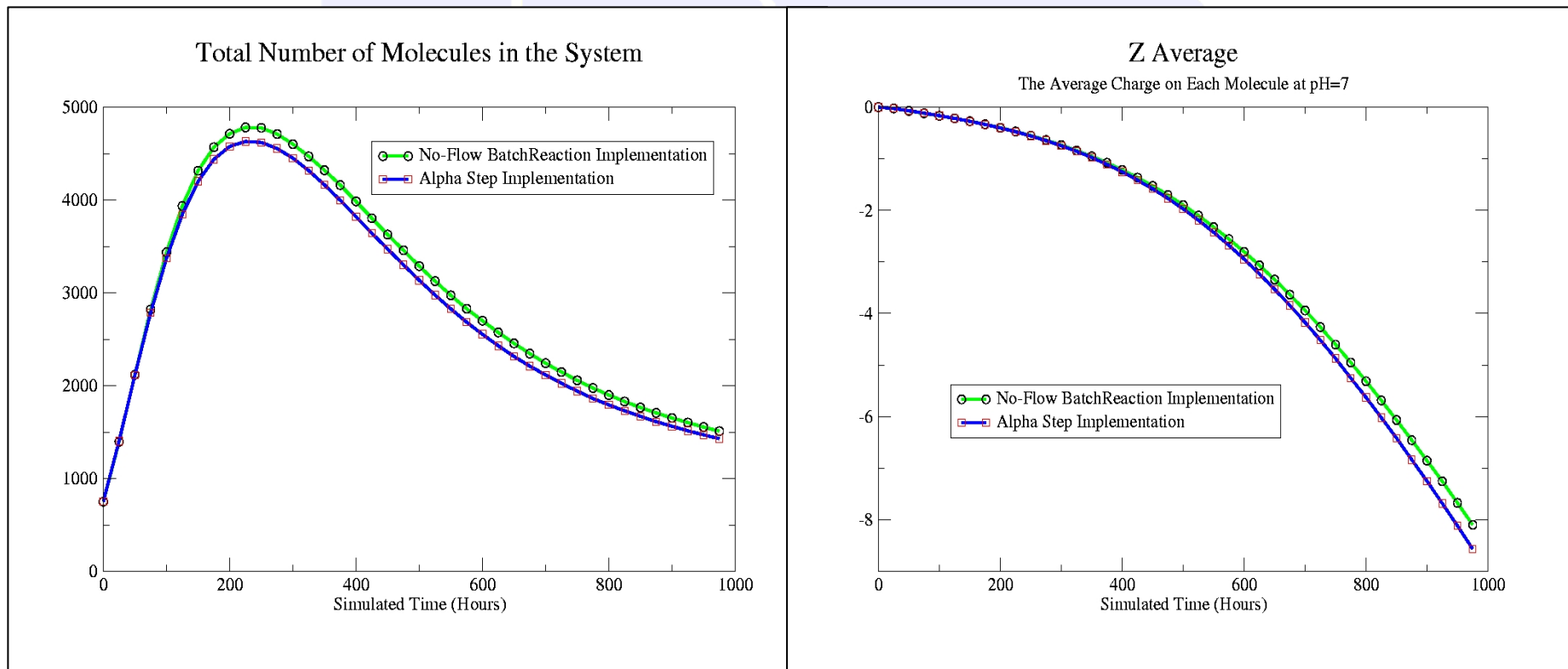
# Case Study 1:

## Model-to-Model Comparison II

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Features	Alpha Step	No-flow Reaction
Developing Group	University of New Mexico, Department of Chemistry	University of Notre Dame, Computer Science and Engineering
Programming language	Pascal	Java (Sun JDK 1.4.2)
Platforms	Delphi 6, Windows	Red hat Linux cluster
Running mode	Standalone	Web based, standalone
Simulation package	None	Swarm, Repast libraries
Animation	None	Yes
Spatial representation	None	2D grid
Second order reaction	Random pick one from list	Choose the nearest neighbor
First order with split	Add to list	Find empty cell nearby

# Case Study 1: Model-to-Model Comparison III

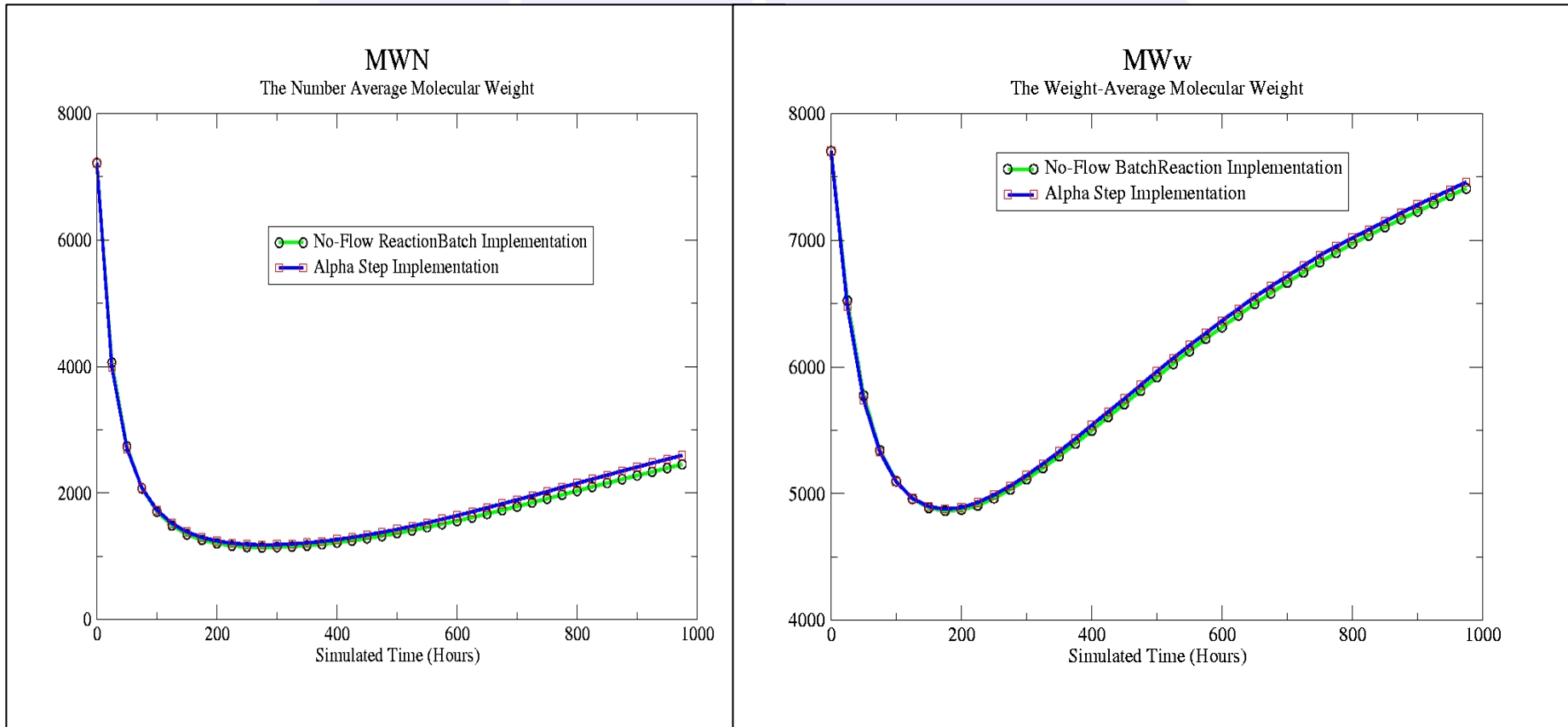


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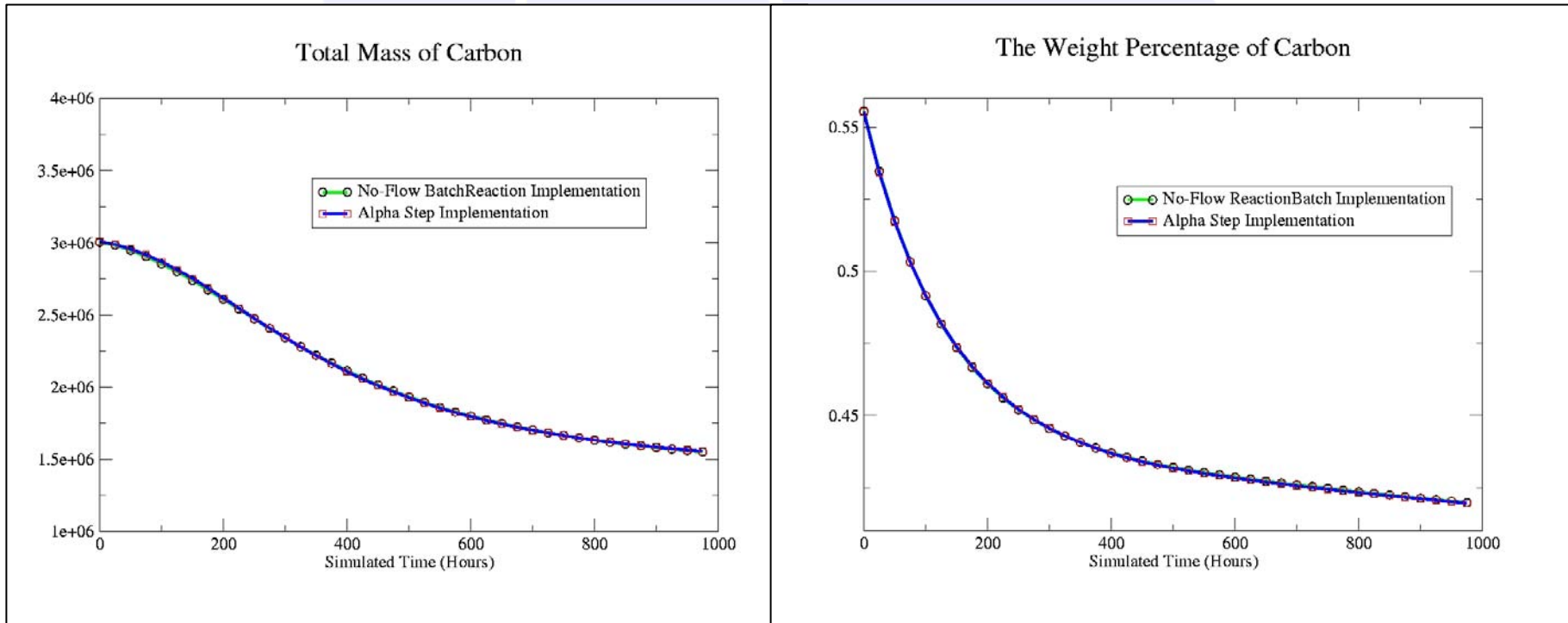
# Case Study 1:

## Model-to-Model Comparison IV

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# Case Study 1: Model-to-Model Comparison V



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# Case Study 2:

## An Economic Model

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### □ Interdisciplinary project

- Initially written in Matlab within Department of Finance
- Converted to C++ by Computer Scientists
- Equation-based system
- Concerned with identifying ideal economic variables, such as debt, money growth, and tax rate

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# Case Study 2: The Conceptual Model

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- Equation-based system
- Nonlinear projection methods used to solve Ramsey problems in a stochastic money economy
- Goal is to generate the best social welfare for a given economy
- Motivation

$$\begin{aligned}\hat{\mu}_{t+1}(\theta_t, g_t, b) &= \sum_{i=1}^{n_g} \sum_{j=1}^{n_g} b_{ij} \Psi_{ij}(\theta_t, g_t), \\ \hat{\tau}_t(\theta_t, g_t, d) &= \sum_{i=1}^{n_g} \sum_{j=1}^{n_g} d_{ij} \Omega_{ij}(\theta_t, g_t), \\ \hat{H}_t(\theta_t, g_t, q) &= \sum_{i=1}^{n_g} \sum_{j=1}^{n_g} q_{ij} \Phi_{ij}(\theta_t, g_t), \\ \hat{\lambda}_{gt}(\theta_t, g_t, v) &= \sum_{i=1}^{n_g} \sum_{j=1}^{n_g} v_{ij} \Gamma_{ij}(\theta_t, g_t).\end{aligned}$$

# Case Study 2: Face Verification

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	<b>LaGrange Multiplier</b>	<b>Labor</b>	<b>Money Growth</b>	<b>Tax Rate</b>	<b>Cash Good</b>	<b>Credit Good</b>
<b>Matlab</b>	0.138	0.309	-0.009	0.188	0.486	0.621
<b>C++</b>	0.138	0.309	-0.009	0.188	0.486	0.621
<b>Steady State</b>	0.138	0.309	-0.009	0.188	0.485	0.620

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# Case Study 2:

## Tracing

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### □ Matlab:

it 44, af 3.7496e-08, rc 0, timer 11.1, l 0.1382704496, m -0.0092286139, t 0.1881024991, h 0.3093668925

cc1 0.4861695543, cc2 0.6212795130, rl 1.0092221442

it 45, af 2.64653e-08, rc 0, timer 11.0, l 0.1382704643, m -0.0092286175, t 0.1881024947, h 0.3093668931

cc1 0.4861695553, cc2 0.6212795120, rl 1.0092221442

### □ C++:

it: 44 af: 0.00144839 rc: 0 l: 0.138359 m: -0.00936025 t: 0.188252 h: 0.309338

cc1: 0.486205 cc2: 0.621244 rl: -0.65888

it: 45 af: 0.00144784 rc: 0 l: 0.138401 m: -0.00937062 t: 0.188239 h: 0.30934

cc1: 0.486208 cc2: 0.621241 rl: -0.665511

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# Case Study 2:

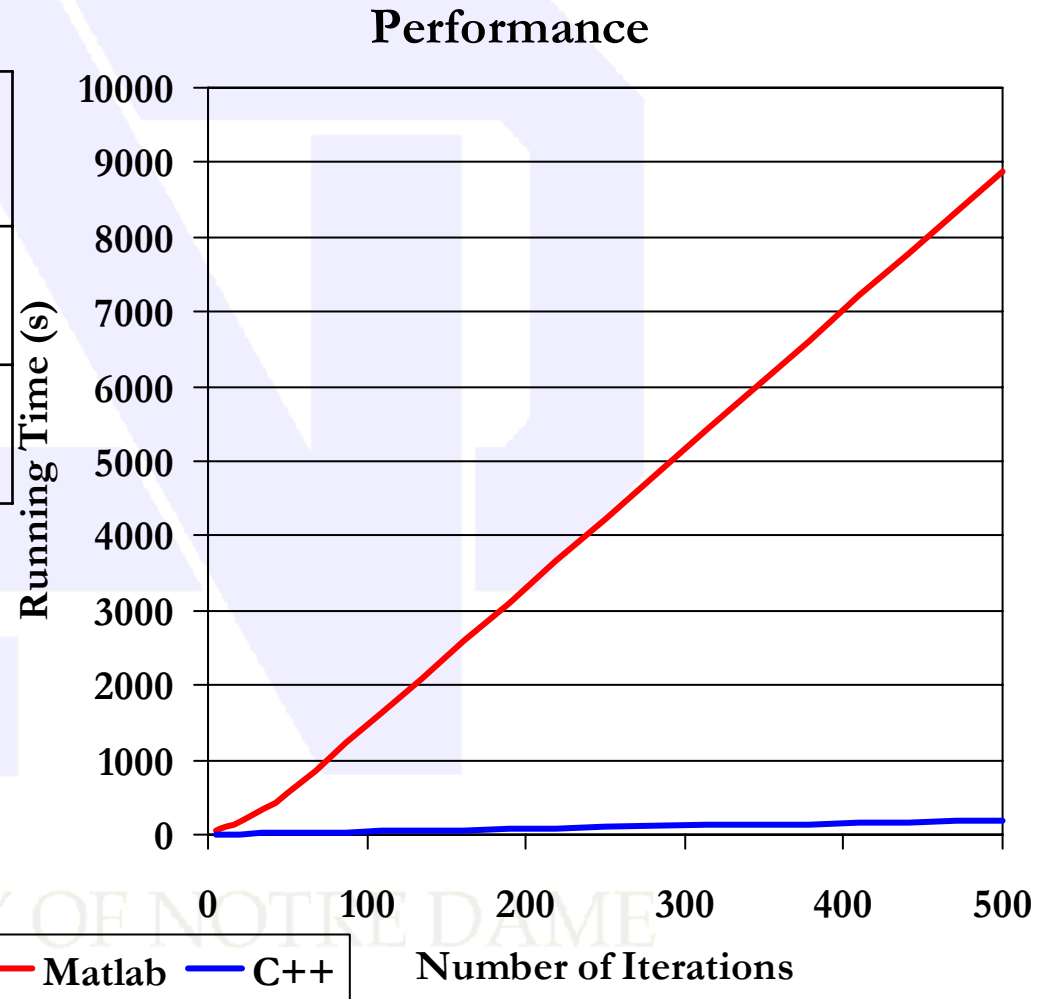
## Implementation Characteristics

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Features	Matlab	C++
Developing Group	University of Notre Dame, Department of Finance	University of Notre Dame, Computer Science and Engineering
Language	High-Level	Lower-Level
Compiler	Interpreted	GNU Compiler
Good For	Prototyping	Speed
Platforms	Linux, Windows	Linux
Running mode	Standalone	Standalone
Packages	LAPACK, etc...	STL
Variables	Implicit	Declared

# Case Study 2: Performance

	5 Iterations	50 Iterations	500 Iterations
Matlab	58 s	568 s	8872 s
C++	2 s	17 s	176 s



# Summary & Conclusion

□ Applied V & V to distinct case studies to increase model confidence

□ Some techniques are more cost-effective

For our models:

	<b>Agent-based</b>	<b>Equation-based</b>
<b>Face Validation/Verification</b>	Very Good	Very Good
<b>Turing Test</b>	Very Good	Good
<b>Internal Validity</b>	Very Good	n/a
<b>Tracing</b>	Fair	Excellent
<b>Black-Box Testing</b>	Good	Good
<b>Model-to-Model Comparison</b>	Very Good	Very Good
<b>Historical Data Verification</b>	Very Good	Very Good
<b>Sensitivity Analysis</b>	Good	Good
<b>Prediction Validation</b>	Good	Fair

# Future Work

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- ❑ Collect and evaluate more statistical data
- ❑ Compare simulation results against empirical data
- ❑ More stringent and formalized V & V
- ❑ Perform more statistical tests

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Questions or Comments?

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