

**Lorentz force**

$$\vec{F} = q\vec{\xi} + q\vec{v} \times \vec{B} = q\vec{\xi} + I\vec{dl} \times \vec{B}$$

**Ampere's law** – differential form

$$\nabla \times \vec{H} = \vec{J} + \frac{d\vec{D}}{dt},$$

a dc current or a displacement current creates a circulating magnetic field.

**Faraday's law** – differential form

$$\nabla \times \vec{E} = -\frac{d\vec{B}}{dt},$$

a time changing magnetic field creates a circulating electric field.

**Stokes theorem**

$$\oint \vec{F} \cdot d\vec{l} = \int_S \nabla \times \vec{F} \cdot d\vec{s}$$

Application of Stokes theorem to Faraday's law yields produces the relationship between electromotive force and magnetic flux,  $\Phi$ , in V s.

$$\int_S \nabla \times \vec{E} \cdot d\vec{S} = -\frac{d}{dt} \int_S \vec{B} \cdot d\vec{S} = -\frac{d\Phi}{dt}$$

$$emf = \oint \vec{E} \cdot d\vec{l} = -\frac{d\Phi}{dt}$$

**Power output of a generator**, ignoring losses,

$$P = V_{emf} I = \frac{upN\Phi}{n} I$$

where  $u$  is the rotational velocity in cycles per second,  $p$  is the number of magnetic poles,  $N$  is the number of active conductors,  $n$  is the number of parallel combinations of wire,  $\Phi$  is the magnetic flux, and  $I$  is the current.

**Energy relations**

$$\text{Potential energy} = mgh$$

$$\text{Kinetic energy} = \frac{1}{2}mv^2$$

$$\text{Rotational energy} = \frac{1}{2}M\omega^2, \text{ where the moment of inertia, } M = \frac{1}{2}mr^2$$

**Solar Cells**

$$I = I_R \left( e^{\frac{qV}{kT}} - 1 \right) - I_{SC}$$

$$\eta = \frac{P_{OUT}}{P_{IN}} = \frac{I_{MAX} V_{MAX}}{P_{IN}} = \frac{FF I_{SC} V_{OC}}{P_{IN}}$$