



Community Detection in the *C. elegans* Connectome

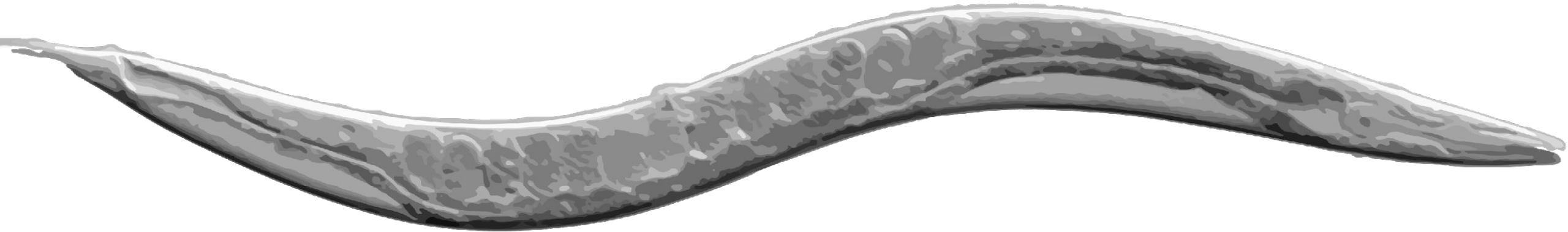
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My Research

Previous work the C. elegans connectome with link analysis

Was curious about community detection in this data set

Currently working on alternative artificial neural network structures that are closer to biology



The Data

280 neurons (humans have 100 billion)

6393 chemical synapses

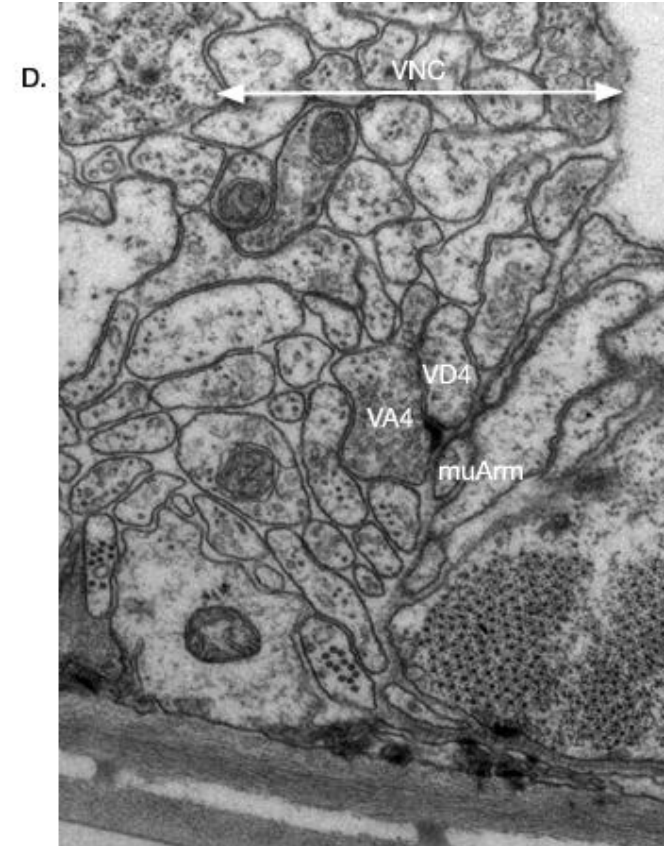
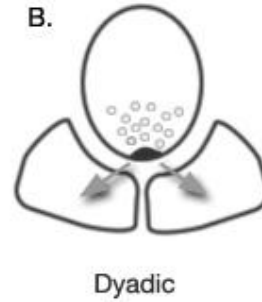
890 electrical junctions

1410 neuromuscular junctions

Neurons can be either Sensory, Inter, Motor, or a combination



Synapses



Characteristics about the graph

Directed

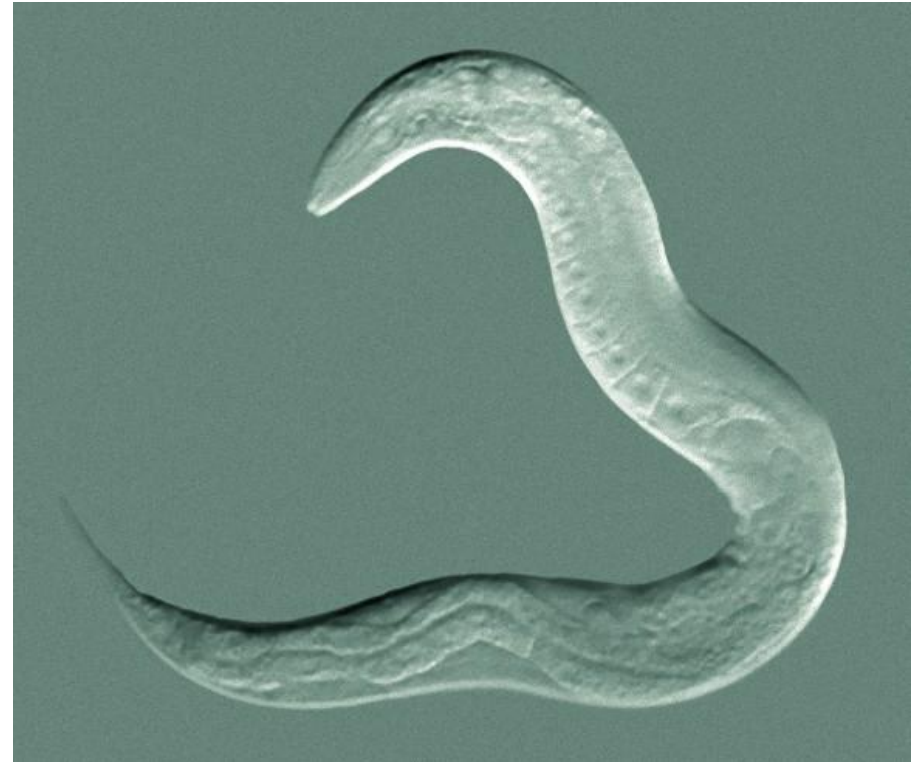
Not a true “Feed Forward Network”

Includes cycles, but no self loops

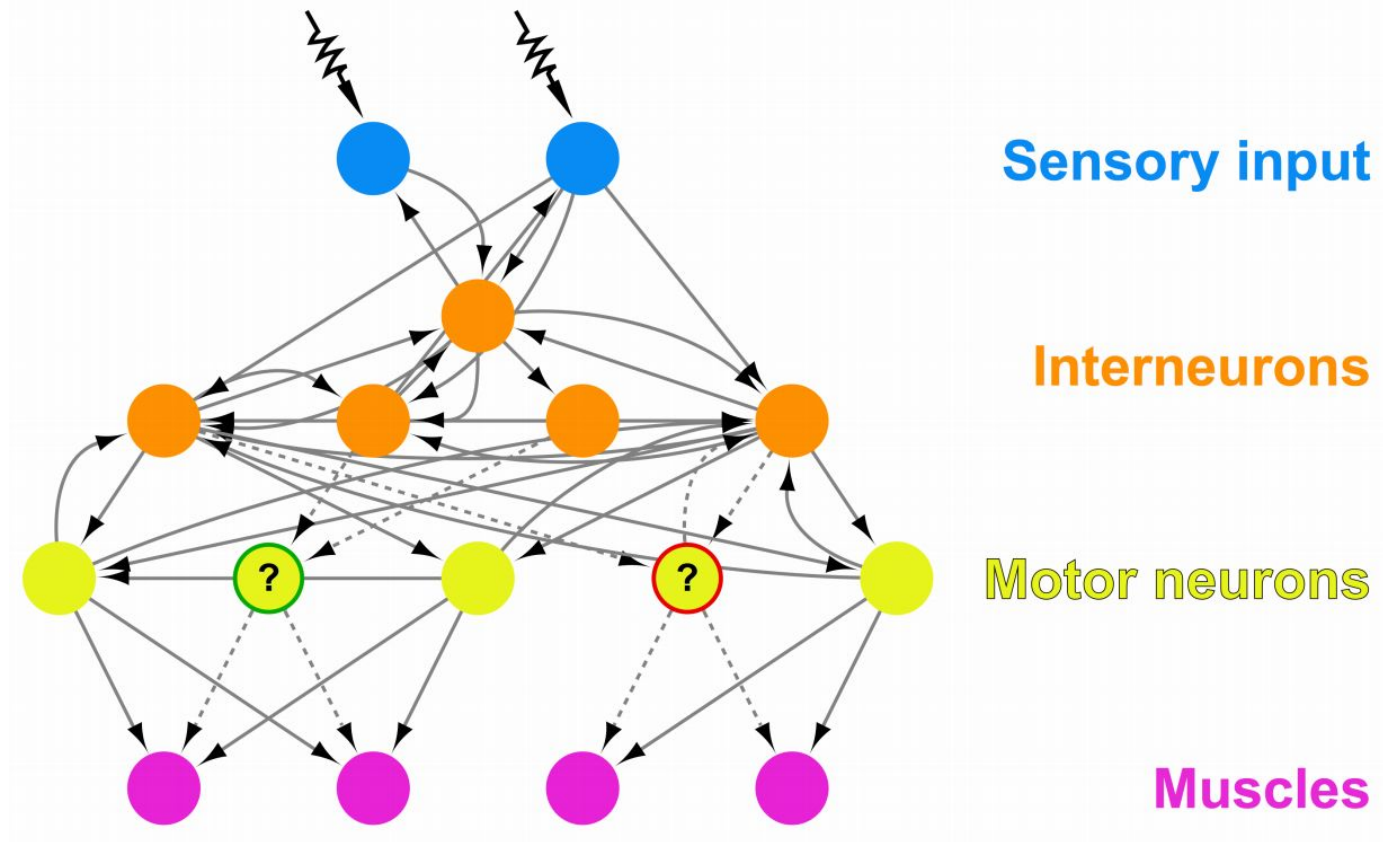
Weighted

Densely connected

Shows a high degree of modularity



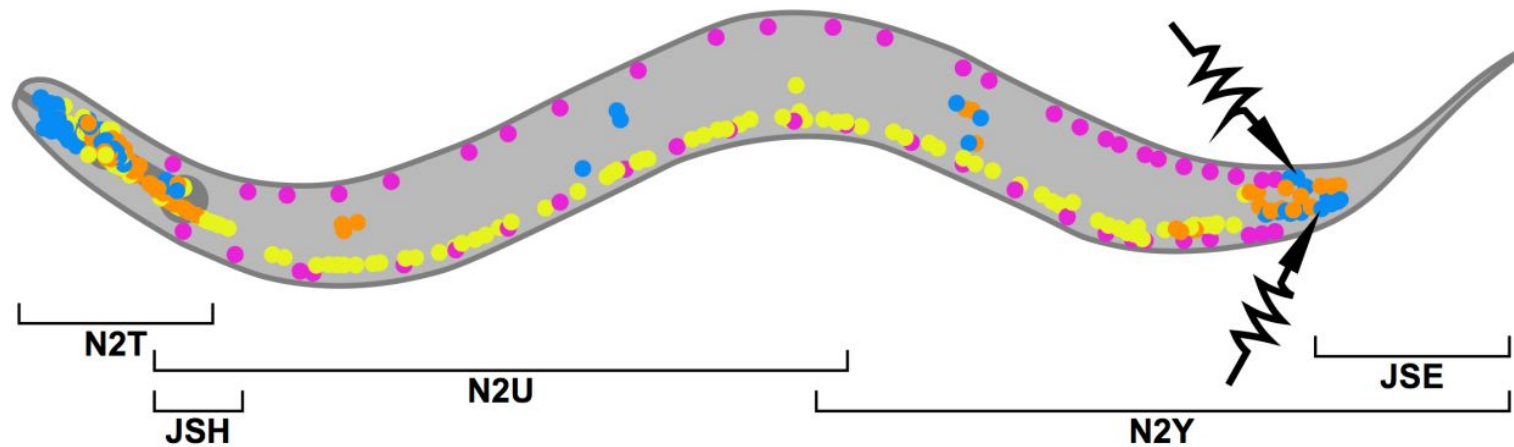
Visualization



More Visualization

<https://elegans.herokuapp.com/>

<http://wormweb.org/neuralnet#c=BAG&m=1>



Modularity

Metric to determine communities

Number between -1 and 1 of how strong communities are

Global Property

Goal: Maximize Modularity

$$Q = \frac{1}{2m} \sum_{ij} \left[A_{ij} - \frac{k_i k_j}{2m} \right] \delta(c_i, c_j),$$

Louvain

Each node starts in a community by itself

Put node i in a neighboring community

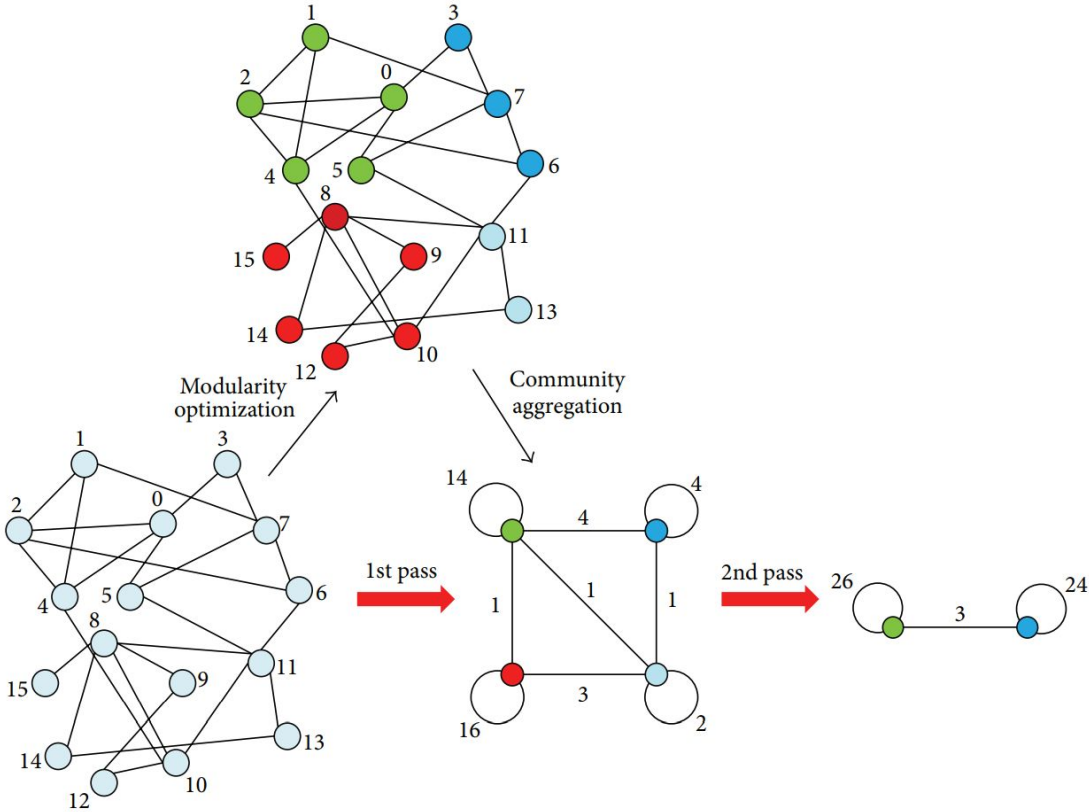
A change in Q is computed:
$$\Delta Q = \left[\frac{\Sigma_{in} + 2k_{i,in}}{2m} - \left(\frac{\Sigma_{tot} + k_i}{2m} \right)^2 \right] - \left[\frac{\Sigma_{in}}{2m} - \left(\frac{\Sigma_{tot}}{2m} \right)^2 - \left(\frac{k_i}{2m} \right)^2 \right]$$

If the change is positive, i becomes part of that community

Once these communities are formed, communities themselves become nodes and intra community weights are treated as self loops, and inter community weights are treated as connections

Repeat

Example



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1:  $V$ : a set of vertices
2:  $E$ : a set of edges
3:  $W$ : a set of weights of edges, initialized to 1
4:  $G \leftarrow (V, E, W)$ 
5: repeat
6:    $C \leftarrow \{\{v_i\} | v_i \in G(V)\}$ 
7:   calculate current modularity  $Q_{cur}$ 
8:    $Q_{new} \leftarrow Q_{cur}$ 
9:    $Q_{old} \leftarrow Q_{new}$ 
10:  repeat
11:    for  $v_i \in V$  do
12:       $Q_{cur} \leftarrow Q_{new}$ 
13:      remove  $v_i$  from its current community
14:       $N_{v_i} \leftarrow \{c_k | v_i \in G(V), v_j \in c_k, e_{ij} \in G(E)\}$ 
15:      find  $c_x \in N_{v_i}$  that has  $\max \Delta Q_{\{v_i\}, c_x} > 0$ 
16:      insert  $v_i$  into  $c_x$ 
17:    end for
18:    calculate new modularity  $Q_{new}$ 
19:  until no membership change or  $Q_{new} = Q_{cur}$ 
20:   $V' \leftarrow \{c_i | c_i \in C\}$ 
21:   $E' \leftarrow \{e_{ij} | \forall e_{ij} \text{ if } v_i \in C_i, v_j \in C_j, \text{ and } C_i \neq C_j\}$ 
22:   $W' \leftarrow \{w_{ij} | \sum w_{ij}, \forall e_{ij} \text{ if } v_i \in C_i \text{ and } v_j \in C_j\}$ 
23:   $G \leftarrow (V', E', W')$ 
24: until  $Q_{new} = Q_{old}$ 

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Pseudocode

$O(N \log N)$

Future Work

Use a directed version of the algorithm

See if the communities form a biological purpose

Make the algorithm work in parallel

