

Analysing the dramatic impact of the bound electron contribution to the index of refraction in plasmas

Joseph Nilsen, Walter R. Johnson

November 17, 2004

Physical Review E

## **Disclaimer**

This document was prepared as an account of work sponsored by an agency of the United States Government. Neither the United States Government nor the University of California nor any of their employees, makes any warranty, express or implied, or assumes any legal liability or responsibility for the accuracy, completeness, or usefulness of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or the University of California. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or the University of California, and shall not be used for advertising or product endorsement purposes.

# Analysing the dramatic impact of the bound electron contribution to the index of refraction in plasmas

Joseph Nilsen and Walter R. Johnson

Lawrence Livermore National Laboratory, Livermore, CA 94551 University of Notre Dame, Notre Dame, IN 46556

#### Abstract

For decades the plasma physics community has relied on the approximation that the index of refraction of a plasma is due solely to the free electrons. This makes the index of refraction less than one and is an essential assumption used in energy deposition in the plasma as well as plasma diagnostics such as interferometers. Recent measurements of Al plasmas using X-ray laser interferometers have observed anomalous results with the index of refraction being larger than one. Subsequent analysis of the experiments showed that the bound electrons could have a larger contribution to the index of refraction with the opposite sign than the free electrons. This effect extends far from the absorption edges and lines of the bound electrons. Utilizing a new average atom code we calculate the index of refraction in C, Al, Ti and Pd plasmas and show that there are many conditions over which the bound electron contribution dominates as we explore photon energies from the optical to 100 eV (12 nm) soft X-rays. During the next decade X-ray free electron lasers and other sources will be available to probe a wider variety of plasmas at higher densities and shorter wavelengths so understanding the index of refraction in plasmas will be even more essential.

PACS codes: 51.70.+f, 52.38.-r, 52.70.-m, 52.70.La

## Introduction

Optical interferometers have been used for many decades to measure the electron density of plasmas [1]. The basic assumption in the data analysis is that the index of refraction of a plasma can be calculated from the free electron density [1-2]. This implies that the number of fringe shifts in the interferometer is directly proportional to the electron density of the plasma. This also makes the index of refraction in the plasma less than one. When X-ray lasers became available, the same assumptions were used as the interferometer was extended to shorter wavelengths in order to probe even higher density plasmas. The first X-ray laser interferometer [3] was demonstrated about 10 years ago using the 15.5 nm Ne-like Y laser at the NOVA facility at Lawrence Livermore National Laboratory (LLNL). Since then, many X-ray laser interferometers [4-6], as well as a high order harmonic interferometer [7], have been used in the wavelength range of 14 to 72 nm. This covers photon energies from 17 to 89 eV.

Experiments recently conducted at the Advanced Photon Research Center at JAERI using the 13.9 nm Ni-like Ag laser [4] and at the COMET laser facility at LLNL using the 14.7 nm Nilike Pd laser [5] observed anomalous behavior of fringe lines in interferometer experiments of Al plasmas where the fringe lines bent in the opposite direction than was expected, indicating the index of refraction was greater than one. Analysis of these experiments showed that the bound electrons have a large contribution to the index of refraction with the opposite sign as the free electrons and can explain how the index of refraction is greater than one in some Al plasmas [8]. The surprising result is that the influence of the bound electrons on the index of refraction extends far from the absorption edges and resonance lines. Resonance lines can affect the index of refraction at photon energies that are located orders of magnitude further removed from the line than the width of the line.

The original analysis [8] of the index of refraction in partially ionized Al plasmas did an individual calculation of the photo-ionization cross section and the dipole allowed lines for each ionization stage of Al. That analysis assumed all the population was in the ground state of each

ionization stage and did not have a distribution of excited states. For Al the analysis adjusted the theoretical calculations so the lines and photo-ionization edges matched the positions measured in experiments. The analysis was done only for a single wavelength, 14.7 nm, which is the wavelength of the Ni-like Pd X-ray laser used in experiments at LLNL [5]. It became clear that we needed the ability to calculate the index of refraction for any plasma at any wavelength.

Fortunately we had available a version of the INFERNO average atom code that is routinely used to calculate the distribution of levels and the absorption coefficient for a given temperature and density [9]. Using a modified version of this code [10], we are now able to calculate the index of refraction for a wide range of plasma conditions. In this work we present results for C, Al, Ti, and Pd plasmas from singly to many times ionized. The index of refraction is calculated for photon energies from 0 to 100 eV (12.4 nm). These calculations enable us to understand under what plasma conditions the free electron approximation is valid and gives us an estimate of the magnitude of the bound electron contribution.

#### Kubo-Greenwood technique for calculating index of refraction

For many years the average-atom technique incorporated in the INFERNO code [9] has been used to calculate the ionization conditions and absorption spectrum of plasmas under a wide variety of conditions. For finite temperatures and densities, the INFERNO code calculates a statistical population for occupation of one-electron Dirac orbitals in the plasma. In this work, we use a non-relativistic version of INFERNO to calculate bound and continuum orbitals and the corresponding self-consistent potential. Applying linear response theory to the average-atom leads to an average-atom version of the Kubo-Greenwood equation [11,12] for the frequencydependent conductivity of the plasma. Molecular orbital versions of the Kubo-Greenwood formula have also been used in recent years to study the conductivity of Al plasmas [13,14]. The imaginary part of the complex dielectric function is proportional to the conductivity. The real part of the dielectric function can be found from its imaginary part using a Kramers-Kronig [15] dispersion relation. With the resulting frequency-dependent dielectric function in hand, optical

properties of the plasma, such as its index of refraction and absorption coefficients, are completely determined from the dielectric function. The details of the Kubo-Greenwood formula applied to the average-atom model will be described in a separate work [10].

#### Traditional analysis of interferometer experiments

The usual formula for the index of refraction of a plasma due to free electrons is  $n = (1 - N_{elec} / N_{erit})^{1/2}$  where  $N_{elec}$  is the electron density of the plasma and  $N_{erit}$  is the plasma critical density. At wavelength  $\lambda$ ,  $N_{erit} = \pi / (r_0 \lambda^2)$  where  $r_0$  is the classical electron radius [2]. Since experiments typically measure an electron density that is much less than the critical density the formula above is approximated by  $n = 1 - (N_{elec} / 2N_{erit})$ . In a typical interferometer experiment [3-7] that probes a uniform plasma of length L using a source with wavelength  $\lambda$ , the number of fringe shifts is equal to  $(1 - n) L / \lambda$ . This assumes that one arm of the interferometer is propagating through vacuum and that one compares the fringe shifts against a set of reference fringes in the absence of any plasma. This also assumes that there is a small angle between the arms of the interferometer so that the cosine of the angle between the two arms can be approximated as 1. With the above approximation for n, the number of fringe shifts equals ( $N_{elec} L$ ) / (2  $\lambda N_{erit}$ ). The experimental analysis is done by simply counting how far the fringes have shifted compared with the reference fringes and converting this into electron density. For the 14.7 nm Pd X-ray laser the number of fringe shifts in the interferometer is ( $N_{elec} L$ ) / (1.5 x 10<sup>19</sup> cm<sup>-2</sup>) and the critical density is 5.17 x 10<sup>24</sup> cm<sup>-3</sup>.

## Analysis of Al plasmas

Since these anomalous index of refraction results were first measured in Al plasmas [4,5] using X-ray laser interferometers we utilize our new tool to analyze some Al plasmas. To simplify the analysis the calculations using the average atom code were done for different temperatures but with a constant ion density of  $10^{20}$  cm<sup>-3</sup>. Since the fringe shifts are proportional to (1 - n) we compare the ratio of  $(1 - n) / (1 - n_{free})$  where  $n_{free}$  is the index of refraction due only to the free electron contribution. If only the free electrons contribute to the index of refraction

this ratio equals one and the traditional analysis is valid. Otherwise this ratio represents the ratio of the measured electron density to the actual electron density when one analyzes the interferometer experiment the traditional way assuming only free electrons contribute to the index of refraction.

Even though the calculations are done for a single ion density the ratio normalizes away the actual density and we would expect the analysis to be valid over a wider range of densities. One limitation of the calculations is that the average atom code assumes the electron, ion, and radiation temperatures are all equal and the plasma's ionization is in local thermodynamic equilibrium (LTE). If one was to calculate a dynamic plasma that was not in equilibrium the ionization condition ( $Z^*$ ) is a better value to compare than the actual temperature of the plasma.  $Z^*$  is the ionization condition of the plasma such that  $Z^* = 1$  means the average ion is singly ionized, 2 means double ionized, etc.

Figure 1(a) shows the ratio  $(1 - n) / (1 - n_{free})$  versus photon energy for an Al plasma with temperature of 2 eV and corresponding  $Z^* = 0.92$ , which means that the average ion is almost singly ionized. Dotted lines are plotted at ratios of 0 and 1 as visual aids. One immediately notices that the ratio is negative from 75 eV to 100 eV with typical values ranging from -1 to -4. This means the index of refraction of the plasmas is greater than one. At 84.46 eV, which is the energy of the Pd X-ray laser (14.68 nm), the ratio is -2.8. In the detailed analysis of Al done in Ref. 8 the ratio for singly ionized Al was -4.2. In both calculations, a Mach-Zehnder or Fresnel bi-mirror interferometer as used in Refs. 4 and 5, would observe the fringes bend the opposite direction than was expected and by a larger distance than would be expected for the electron density being measured. Looking at lower energies, such as the 26.4 eV (46.9 nm) of the Ne-like Ar X-ray laser [6] that has been used for many interferometer experiments, the ratio is 2.6. An interferometer built at this wavelength would measure an electron density that was 2.6 times larger than the actual density. It is striking that the ratio crosses one but differs significantly from one over most of this energy range. Even at low energies, such as 4.68 eV, which is the energy of

the 4<sup>th</sup> harmonic of the 1.06  $\mu$ m Nd laser, the ratio is predicted to be –3.0. Now it is important to recognize that an average atom calculation will not have the position of the absorption lines and edges accurate enough to use the ratio to quantitatively analyze the experiments but it is an invaluable first step in understanding the validity of the experiments and approximating the potential corrections needed to understand the experiments.

Figure 1(b) plots the ratio versus photon energy for an Al plasma with temperature of 5 eV and  $Z^* = 2.12$ , which means it is slightly more than doubly ionized, on average. At energies below 40 eV the ratio is close to unity but near 84 eV the ratio has very strong oscillations because of the presence of strong lines. The structure is sufficiently complex and highlights how a quantitative analysis needs to know the exact positions of the absorption lines very accurately.

In Fig. 1(c) we plot the ratio for a 10 eV Al plasma with  $Z^* = 2.88$ , which is almost triply ionized Ne-like Al. In Ne-like Al the strong 3s - 2p resonance lines are centered at 16.08 nm or 77.07 eV [16]. This figures shows a strong feature at 73.0 eV due to these absorption lines. One can obtain a more accurate estimate of the ratio by shifting this feature a few eV to agree with the experimentally observed values of the lines as was done for the detailed analysis in Ref. 8. In Fig. 1(c) the ratio at 84.46 eV is -2.4 but reduces to -0.9 if one shifts the spectrum by 4.07 eV to match the position of the Ne-like resonance line. Ref. 8 predicted a ratio of -0.6 for triply ionized Al at this photon energy. All three analyses predict that the ratio is negative and that the index of refraction is greater than one. This is consistent with the fringe lines in an interferometer experiment bending the opposite direction than expected.

Another important plasma property to consider is the absorption coefficient of the plasma since the x-rays or optical photons need to be able to penetrate the plasma to be useful for interferometer measurements. Figure 2 shows the absorption coefficient versus photon energy for an Al plasma of temperature 10 eV with an ion density of 10<sup>20</sup> cm<sup>-3</sup>. For the region between 75 and 85 eV and also between 40 and 70 eV the absorption coefficient is less than 10 cm<sup>-1</sup>. Since a typical interferometer experiment uses a 0.1 cm long plasma, this means the plasma will be

optically thin to the X-rays. Again, keep in mind that the spectra needs to be shifted about 5 eV to higher energy to agree with the experiments, so even the 89 eV Ag X-ray laser used in the experiments in Ref. 4 would have low absorption under these conditions.

As we continue to ionize the Al plasma Fig, 3(a) shows the ratio  $(1 - n) / (1 - n_{free})$  versus photon energy for a 20 eV Al plasma with Z\* = 4.64. Much of the complicated structure is disappearing at energies near 84 eV but the ratio is still only 0.6 and is in very good agreement with the value of 0.5 that one interpolates from Ref. 8. In this case the fringes would bend the expected direction in an interferometer experiment but the measured value of the electron density would be low by 40 to 50%.

Finally, Fig. 3(b) shows the ratio for a 40 eV Al plasma with  $Z^* = 7.64$ . While the ratio is not exactly one, it is within 10% of unity for most of the figure with the exception of some weak resonances. One had to ionize almost 8 of the 13 electrons from Al in order to approach the free electron approximation for the index of refraction. This is the same conclusion reached in Ref. 8. The Al experiments highlight how the traditional equation for the index of refraction in a plasma is not valid over a large range of plasma conditions and photon energies. At optical photon energies near a few eV the free electron approximation to the index for Al plasmas does appear to be valid except for the single ionized case.

## Analysis of other plasmas using carbon, titanium, or palladium

Since plastics and other materials containing carbon are commonly used in experiments we decided to look at the index of refraction in carbon plasmas. Again we fix the ion density of the plasma at  $10^{20}$  cm<sup>-3</sup>. Figure 4 plots the ratio  $(1 - n) / (1 - n_{free})$  versus photon energy for C plasmas with temperatures ranging from 2 to 20 eV and the corresponding Z\* ranging from 0.58 to 3.97. One notices that the figure is very complicated for photon energies below 50 eV. If we focus on the 84.46 eV energy of the Pd X-ray laser used in the interferometer experiments [5] at LLNL one observes that the ratio can be much larger than unity at low ionization states of C. This would result in an experiment that greatly overestimates the electron density of the plasma.

Even at 10 eV, where the plasma is almost triply ionized, the ratio is 1.3 from 60 to 100 eV so experiments done with these energies would overestimate the electron density by 30%. The C plasma at 40 eV, which is almost 4 times ionized, has a ratio of 0.96 for energies above 60 eV and is close to 1 over the whole range with a few small oscillations. The C plasma needs to be ionized down to the K shell before the free electron contribution dominates the index of refraction in this energy range. Keep in mind that if we look at higher photon energies near the K edges the ratio will again deviate substantially from 1.

Ti plasmas have been studied for many reasons including their use as X-ray lasers [17]. Figure 5(a) shows the ratio  $(1 - n) / (1 - n_{free})$  versus photon energy for several Ti plasmas with temperatures of 5 and 40 eV. Again we fix the ion density of the plasma at  $10^{20}$  cm<sup>-3</sup>. At 5 eV the plasma is about doubly ionized and the ratio is about 4 over the 80 to 100 eV photon range, meaning an interferometer experiment using this photon energy would overestimate the electron density by a factor of 4. One needs to be almost 10 times ionized, as shown for the 40 eV curve, to have the ratio approach one over most of the plot. Even then there is a resonance near 100 eV that significantly changes the results if you are close enough to this weak resonance. Figure 5(b) shows the ratio for a 20 eV Ti plasma with  $Z^* = 6.2$ . A dotted line is shown with value one as a visual aid. The figure is rich in structure and shows how complicated it is to analyze a Ti plasma under these conditions.

Pd has been used very successfully as an X-ray laser for many years. Recently experiments [18] have been done to measure the plasma conditions of the Ni-like Pd X-ray laser just prior to lasing. The Pd laser is created by first using a prepulse to illuminate a solid target. The target heats and expands to create a plasma at the correct density and ionization to lase. The prepulse is followed by a short, high-intensity pulse that rapidly heats the plasma to lasing conditions and ionizes regions of the plasma that are slightly under-ionized to create the 18 times ionized Ni-like Pd plasma. Figure 6(a) shows the ratio  $(1 - n) / (1 - n_{free})$  versus photon energy for Pd plasmas at 20 and 80 eV with Z\* = 7.2 and 17.8 respectively. Again we fix the ion density

of the plasma at  $10^{20}$  cm<sup>-3</sup>. At 84.46 eV the ratio is 2.6 for the 20 eV plasma but is 1.0 for the 80 eV plasma. This figure shows how even 7 times ionized Pd has a large contribution from the bound electrons to the index of refraction. By the time the plasma is near Ni-like Pd the ratio approaches one over this entire energy range except for some small resonances. Since the Pd plasma may be a few times less ionized than Ni-like in the interferometer experiments [18] that measure the condition of the Pd plasma created by the prepulse, Fig. 6(b) shows the ratio for a 60 eV Pd plasma with Z\* = 15.4. A dotted line at one is plotted as a visual aid. At 84.46 eV the ratio is 1.05 so the interferometer experiments could have a small overestimate of about 5% if the plasma is only 15 times ionized. This is an example of using the average atom code to validate that the interferometer experiments are being done in a regime of validity for the free electron approximation to the index of refraction. This also enables us to estimate the magnitude of the contribution from the bound electrons.

## Conclusions

We have discussed the large contribution that the bound electrons can make to the index of refraction in a plasma over the photon range from the optical up to 100 eV (12 nm) soft Xrays. For decades the analysis of plasma diagnostics such as interferometers have relied on the approximation that the index of refraction of a plasma is due solely to the free electrons. This makes the index of refraction less than one and is also an essential assumption used in energy deposition in the plasma and for photon transport calculations. Recent measurements of Al plasmas using X-ray laser interferometers observed anomalous results with the index of refraction being larger than one. The analysis of the Al plasmas show that the bound electrons can have the dominant contribution to the index of refraction from both absorption edges and lines. It was well known that a strong resonance line can cause anomalous results near the wings of an absorption line but this work shows that the effects from the lines can extend to energies that are orders of magnitude further removed from the line than the width of the line. Similar long-range effects are shown for the absorption edges. Utilizing a new average atom code we calculate the index of refraction in C, Al, Ti and Pd plasmas and show many conditions over which the bound electron contribution dominates the free electrons as we explore photon energies from the optical to 100 eV (12 nm) soft X-rays. During the next decade X-ray free electron lasers and other sources will be available to probe a wider variety of plasmas at higher densities and shorter wavelengths so it will be even more essential to understand the index of refraction in plasmas.

### Acknowledgements

The authors would like to thank K. T. Cheng who made valuable suggestions in the process of preparing this work. This work was performed under the auspices of the U. S. Department of Energy by the University of California Lawrence Livermore National Laboratory under contract No.W-7405-ENG-48. This research was also sponsored by the National Nuclear Security Administration under the Stewardship Science Academic Alliances program through U. S. Department of Energy Research Grant # DE-FG03-02NA00062.

#### References

- [1] G. J. Tallents, J. Phys. D. 17, 721-732 (1984).
- [2] H. R. Griem, *Principles of Plasma Spectroscopy*, (Cambridge University Press, Cambridge, 1997) p. 9
- [3] L. B. Da Silva, T. W. Barbee, Jr., R. Cauble, P. Celliers, D. Ciarlo, S. Libby, R. A. London, D. Matthews, S. Mrowka, J. C. Moreno, D. Ress, J. E. Trebes, A. S. Wan, and F. Weber, Phys. Rev. Lett. 74, 3991–3994 (1995).
- [4] H. Tang, O. Guilbaud, G. Jamelot, D. Ros, A. Klisnick, D. Joyeux, D. Phalippou, M. Kado, M. Nishikino, M. Kishimoto, K. Sukegawa, M. Ishino, K. Nagashima, and H. Daido, Appl. Phys. B 78, 975 977 (2004).
- [5] J. Filevich, J. J. Rocca, M. C. Marconi, S. Moon, J. Nilsen, J. H. Scofield, J. Dunn, R. F. Smith, R. Keenan, J. R. Hunter, and V. N. Shlyaptsev, "Observation of a multiply ionized plasma with index of refraction greater than one," University of California report UCRL-JRNL-207242, submitted to Phys. Rev. Lett. (2004).
- [6] J. Filevich, K. Kanizay, M. C. Marconi, J. L. A. Chilla, and J. J. Rocca, Opt. Lett 25, 356 (2000).
- [7] D. Descamps, C. Lyngå, J. Norin, A. L'Hullier, C.-G. Wahlström, J.-F. Hergott, H. Merdji,
  P. Salières, M. Bellini, and T. W. Hänsch, Opt. Lett. 25, 135 (2000).
- [8] Joseph Nilsen and James H. Scofield, Opt. Lett. 29, 2677 (2004).
- [9] D. A. Liberman, J. Quant. Spectrosc. Radiat. Transfer 27, 335 (1982).
- [10] W. R. Johnson, C. Guet, and G. F. Bertsch, "Optical properties of plasmas based on an average-atom model," submitted for publication to J. Quant. Spectrosc. Radiat. Transfer (2004).
- [11] D. A. Greenwood, Proc. Phys. Soc. London 715, 585 (1958).
- [12] R. Kubo, J. Phys. Soc. Jpn. 12, 570 (1957).
- [13] M. P. Desjarlais and J. D. Kress and L. A. Collins, Phys. Rev. E 66, 025401(R) (2002).
- [14] V. Recoules and P. Renaudin and J. Clèouin and P. Noiret and G. Zèrah, Phys. Rev. E 66, 056412 (2002).

- [15] L. D. Landau and E. M. Lifshitz, *Electrodynamics of Continuous Media*, (Pergamon, New York, 1984) pp. 280 - 283
- [16] R. L. Kelly, J. Phys. Chem Ref. Data 16, Suppl. 1, 223 (1987).
- [17] Joseph Nilsen, Brian J. MacGowan, Luiz B. Da Silva, and Juan C. Moreno, Phys. Rev. A 48, 4682 (1993).
- [18] R.F. Smith, J. Dunn, J. Filevich, S. Moon, J. Nilsen, R. Keenan, V.N. Shlyaptsev, J.J. Rocca, J.R. Hunter, R. Shepherd, R. Booth, and M.C. Marconi, "Improved energy coupling into the gain region of the Ni-like Pd transient collisional x-ray laser," submitted to Phys. Rev. Lett. (2004).

## **Figure Captions**

Fig. 1. Ratio  $(1-n) / (1-n_{free})$  versus photon energy for Al plasmas with temperatures of (a) 2 eV, (b) 5 eV, and (c) 10 eV. The corresponding ionization is  $Z^* = 0.92$ , 2.12, and 2.88, respectively. The ion density is  $10^{20}$  cm<sup>-3</sup>. The dotted lines at ratios of 0 and 1 are visual aids.

Fig. 2. Absorption coefficient versus photon energy for an Al plasma with temperature of 10 eV. The ion density is  $10^{20}$  cm<sup>-3</sup>.

Fig. 3. Ratio (1-n) / (1-n<sub>free</sub>) versus photon energy for Al plasmas with temperatures of (a) 20 eV and (b) 40 eV. The corresponding ionization is  $Z^* = 4.64$  and 7.64, respectively. The ion density is  $10^{20}$  cm<sup>-3</sup>. The dotted line at a ratio of 1 is a visual aid.

Fig. 4. Ratio  $(1-n) / (1-n_{free})$  versus photon energy for C plasmas with temperatures of 2, 5, 10, and 20 eV. The corresponding ionization Z\* ranges from 0.58 to 3.97. The ion density is  $10^{20}$  cm<sup>-3</sup>.

Fig. 5. (a) Ratio  $(1-n) / (1-n_{free})$  versus photon energy for 5 and 40 eV Ti plasmas with  $Z^* = 2.2$  and 9.9, respectively. (b) Ratio for Ti plasma with temperature of 20 eV and  $Z^* = 6.2$ . The dotted lines at ratios of 0 and 1 are visual aids. The ion density is  $10^{20}$  cm<sup>-3</sup> for all the Ti plasmas.

Fig. 6. (a) Ratio  $(1-n) / (1-n_{free})$  versus photon energy for 20 and 80 eV Pd plasmas with  $Z^* = 7.2$  and 17.8, respectively. (b) Ratio for Pd plasma with temperature of 60 eV and  $Z^* = 15.4$ . The dotted line at a ratio of 1 is a visual aid. The ion density is  $10^{20}$  cm<sup>-3</sup> for all the Pd plasmas.



Fig. 1. Ratio  $(1-n) / (1-n_{free})$  versus photon energy for Al plasmas with temperatures of (a) 2 eV, (b) 5 eV, and (c) 10 eV. The corresponding ionization is Z\* = 0.92, 2.12, and 2.88, respectively. The ion density is  $10^{20}$  cm<sup>-3</sup>. The dotted lines at ratios of 0 and 1 are visual aids.



Fig. 2. Absorption coefficient versus photon energy for an Al plasma with temperature of 10 eV. The ion density is  $10^{20}$  cm<sup>-3</sup>.



Fig. 3. Ratio  $(1-n) / (1-n_{free})$  versus photon energy for Al plasmas with temperatures of (a) 20 eV and (b) 40 eV. The corresponding ionization is  $Z^* = 4.64$  and 7.64, respectively. The ion density is  $10^{20}$  cm<sup>-3</sup>. The dotted line at a ratio of 1 is a visual aid.



Fig. 4. Ratio  $(1-n) / (1-n_{free})$  versus photon energy for C plasmas with temperatures of 2, 5, 10, and 20 eV. The corresponding ionization Z\* ranges from 0.58 to 3.97. The ion density is  $10^{20}$  cm<sup>-3</sup>.



Fig. 5. (a) Ratio (1-n) / (1-n<sub>free</sub>) versus photon energy for 5 and 40 eV Ti plasmas with  $Z^* = 2.2$  and 9.9, respectively. (b) Ratio for Ti plasma with temperature of 20 eV and  $Z^* = 6.2$ . The dotted lines at ratios of 0 and 1 are visual aids. The ion density is  $10^{20}$  cm<sup>-3</sup> for all the Ti plasmas.



Fig. 6. (a) Ratio (1-n) / (1-n<sub>free</sub>) versus photon energy for 20 and 80 eV Pd plasmas with  $Z^* = 7.2$  and 17.8, respectively. (b) Ratio for Pd plasma with temperature of 60 eV and  $Z^* = 15.4$ . The dotted line at a ratio of 1 is a visual aid. The ion density is  $10^{20}$  cm<sup>-3</sup> for all the Pd plasmas.