

# Optical Properties of Plasmas Based on an Average-Atom Model

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- Linear Response  $\Rightarrow$  Kubo-Greenwood formula for  $\sigma(\omega)$
- Kramers-Kronig Dispersion Relation  $\Rightarrow$  Dielectric Function  $\epsilon(\omega)$
- Index of refraction  $n(\omega) + i\kappa(\omega) = \sqrt{\epsilon(\omega)}$

## Motivation

Free electron formula for index of refraction is used to determine electron densities.

$$n = \sqrt{1 - \frac{\omega_0^2}{\omega^2}} \approx 1 - \frac{\omega_0^2}{2\omega^2} < 1 \quad \text{where} \quad \omega_0^2 = 4\pi \frac{e^2}{m} \frac{N_{\text{free}}}{\Omega}$$

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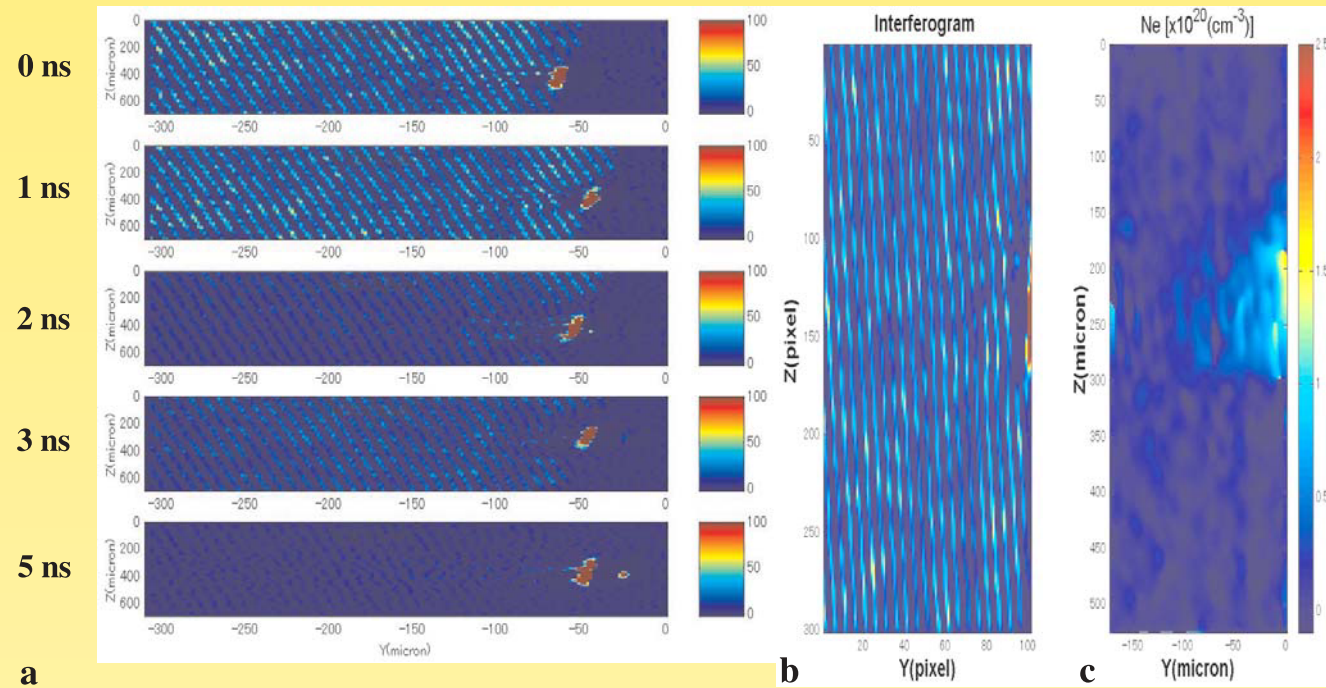
**Reason:** Effect of bound electrons on optical properties.

- LLNL COMET laser facility<sup>1</sup> (14.7 nm Ni-like Pd laser)
- Advanced Photon Research Center JAERI<sup>2</sup> (13.9 nm Ni-like Ag laser)

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<sup>1</sup>J. Filevich et al. *Proceedings of the 9th International Conference on X-Ray Lasers*, May 23-28 (2004)

<sup>2</sup>H. Tang et al., *Appl. Phys.* **B78**, 975 (2004)



**FIGURE 2** **a** Interference fringes after removing self-emission of the Al plasma. The fringes evolve with the increasing of diagnosing delay (0 ~ 5 ns). Only the fringes very close to the target surface cannot be resolved due to the over intense self-emission. **b** Interference fringe pattern **c** Electron density map for the 1 ns-delay and for an irradiance of  $1.4 \times 10^{11} \text{ Wcm}^{-2}$

## Average-Atom Model

QM version of a model proposed by Feynman, Metropolis, and Teller<sup>3</sup>

Inside a neutral Wigner-Seitz cell:  $\Omega = A / (\text{Avagadro No.} \times \text{density})$

$$\left[ \frac{p^2}{2m} - \frac{Z}{r} + V \right] \psi_i(\mathbf{r}) = \epsilon_i \psi_i(\mathbf{r}) \quad (1)$$

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$V = V_{\text{dir}}(r) + V_{\text{exc}}(r)$  for  $r \leq R$  and  $V = 0$  otherwise.

$$\nabla^2 V_{\text{dir}} = -4\pi\rho \quad (2)$$

$V_{\text{exc}}(\rho)$  is given in the local density approximation

---

<sup>3</sup>R. P. Feynman, N. Metropolis and E. Teller, Phys. Rev. **75** 1561 (1949)

## Thermal Average Electron Density

Contributions to the density are

$$\rho_b(r) = \frac{1}{4\pi r^2} \sum_l 2(2l + 1) \sum_n f(\epsilon_{nl}) P_{nl}(r)^2 \quad (3)$$

$$\rho_c(r) = \frac{1}{4\pi r^2} \sum_l 2(2l + 1) \int_0^\infty d\epsilon f(\epsilon) P_{\epsilon l}(r)^2 \quad (4)$$

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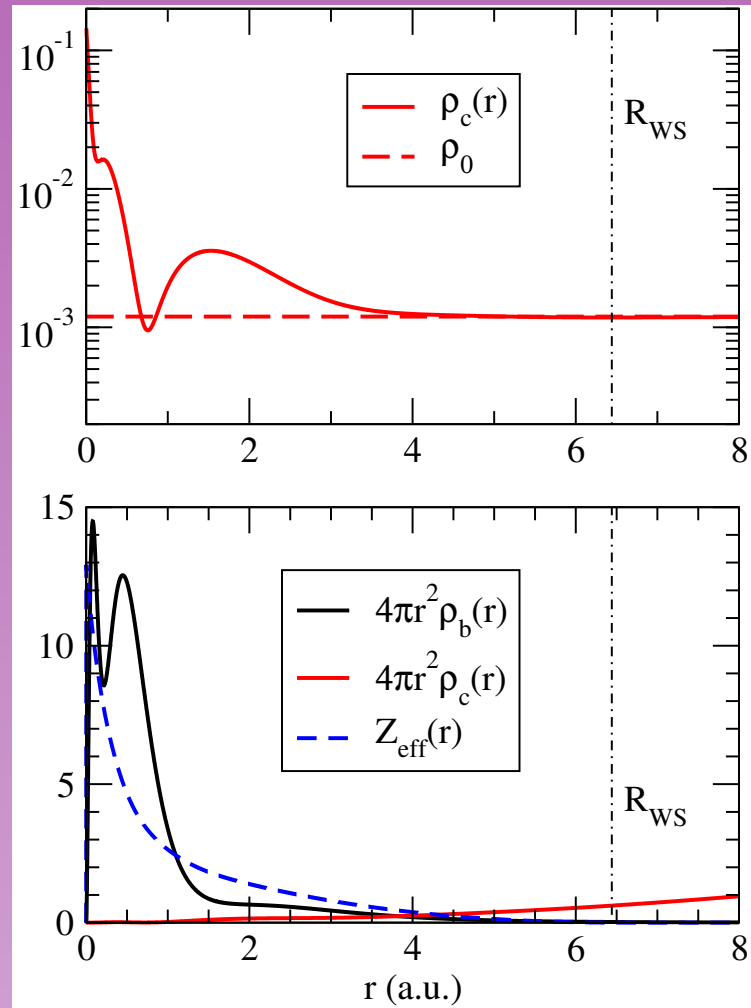
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Eqs. (1-5) are solved self-consistently for  $\rho$ ,  $V$ , and  $\mu$ .

## Example

Al: density 0.27 gm/cc,  $T = 5$  eV,  $R = 6.44$  a.u.,  $\mu = -0.3823$  a.u.

| Bound States |         |         |       | Continuum States |          |               |
|--------------|---------|---------|-------|------------------|----------|---------------|
| State        | Energy  | $n(l)$  | $l$   | $n(l)$           | $n_0(l)$ | $\Delta n(l)$ |
| $1s$         | -55.189 | 2.0000  | 0     | 0.1090           | 0.1975   | -0.0885       |
| $2s$         | -3.980  | 2.0000  | 1     | 0.2149           | 0.3513   | -0.1364       |
| $2p$         | -2.610  | 6.0000  | 2     | 0.6031           | 0.3192   | 0.2839        |
| $3s$         | -0.259  | 0.6759  | 3     | 0.2892           | 0.2232   | 0.0660        |
| $3p$         | -0.054  | 0.8300  | 4     | 0.1514           | 0.1313   | 0.0201        |
|              |         |         | 5     | 0.0735           | 0.0674   | 0.0061        |
|              |         |         | 6     | 0.0326           | 0.0308   | 0.0018        |
|              |         |         | 7     | 0.0132           | 0.0127   | 0.0005        |
|              |         |         | 8     | 0.0049           | 0.0048   | 0.0001        |
|              |         |         | 9     | 0.0017           | 0.0016   | 0.0001        |
|              |         |         | 10    | 0.0005           | 0.0005   | 0.0000        |
|              | Nbound  | 11.5059 | Nfree | 1.4941           | 1.3404   | 0.1537        |



## Pressure

$$P = \frac{1}{3} [T_{xx} + T_{yy} + T_{zz}] \Big|_{r=R}$$
$$\approx \frac{(2mkT)^{5/2}}{6m\pi^2} I_{3/2}(\mu/kT),$$

where  $I_k(x)$  is a “Fermi-Dirac” integral

$$I_k(x) = \int_0^\infty \frac{y^k dy}{1 + e^{(y-x)}}$$

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$P = P(\Omega, T)$  provides an **equation of state** for the plasma

n.b. atomic unit of  $[P]$ : 294.21 Mbar.

## Kinetic and Potential Energies

$$\begin{aligned} E_{\text{kin}} &= \int d^3r \sum_i \langle \psi_i | \frac{p^2}{2m} | \psi_i \rangle f(\epsilon_i) \\ &= \frac{3}{2} P \Omega - \frac{1}{2} E_{\text{pot}} \end{aligned}$$

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This is the **generalized virial theorem**.

## Entropy

The entropy  $S$  of a collection of fermions is given by the expression

$$TS = -kT \sum_i \{f(\epsilon_i) \ln f(\epsilon_i) + [1 - f(\epsilon_i)] \ln [1 - f(\epsilon_i)]\}$$

where  $f(\epsilon_i) = 1 / [1 + \exp(\epsilon_i - \mu) / kT]$

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where  $f(\epsilon_i) = 1 / [1 + \exp(\epsilon_i - \mu)/kT]$  This can be manipulated to give

$$\begin{aligned} TS &= \frac{5}{3}E_{\text{kin}} + E_{e-n} + 2E_{e-e} - \mu N \\ &= \frac{5}{2}P\Omega + \frac{1}{6}E_{e-n} + \frac{7}{6}E_{e-e} - \mu N \end{aligned}$$

## Other Thermodynamic Quantities

The internal energy  $U$  and the Helmholtz free energy  $F$  are given by

$$U = E_{\text{kin}} + E_{\text{pot}} = \frac{3}{2}P\Omega + \frac{1}{2}E_{e-n} + \frac{1}{2}E_{e-e}$$

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$$dU = dQ - Pd\Omega = TdS - Pd\Omega$$

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The Helmholtz free energy is a thermodynamic function of the “natural” variables of the problem,  $\Omega$  and  $T$ :

$$S = -\left.\frac{\partial F}{\partial T}\right|_{\Omega} \quad P = -\left.\frac{\partial F}{\partial \Omega}\right|_T$$

## Application: Plasma Conductivity

The Ziman formula<sup>4</sup> for the *static* conductivity of a many-particle system is

$$\sigma = -\frac{2e^2}{3} \int \frac{d^3p}{(2\pi)^3} v^2 \tau(p) \frac{\partial f}{\partial E},$$

where  $\tau(p)$  is the mean collision time and where  $f(E)$  is the Fermi function.

$$\tau(p) = \frac{\Lambda(p)}{v}$$

$$\Lambda(p) = \frac{\Omega}{\sigma_{\text{tr}}(p)}$$

$$\sigma_{\text{tr}}(p) = \frac{4\pi}{p^2} \sum_{l=0}^{\infty} (l+1) \sin^2(\delta_{l+1} - \delta_l)$$

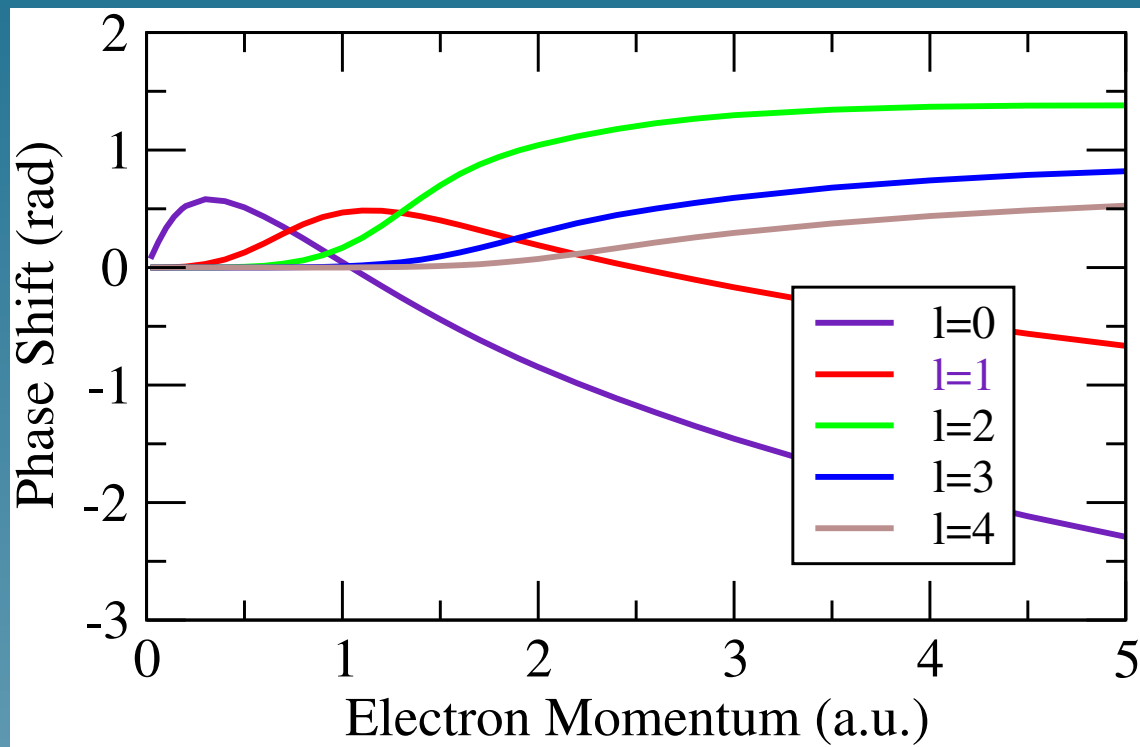
$$\tau(p) = \frac{\Omega}{v \sigma_{\text{tr}}(p)}$$

$$\sigma = -\frac{\Omega}{3\pi^2} \int_0^{\infty} dE \left[ \frac{v^2}{\sigma_{\text{tr}}(p)} \right] \frac{\partial f}{\partial E}.$$

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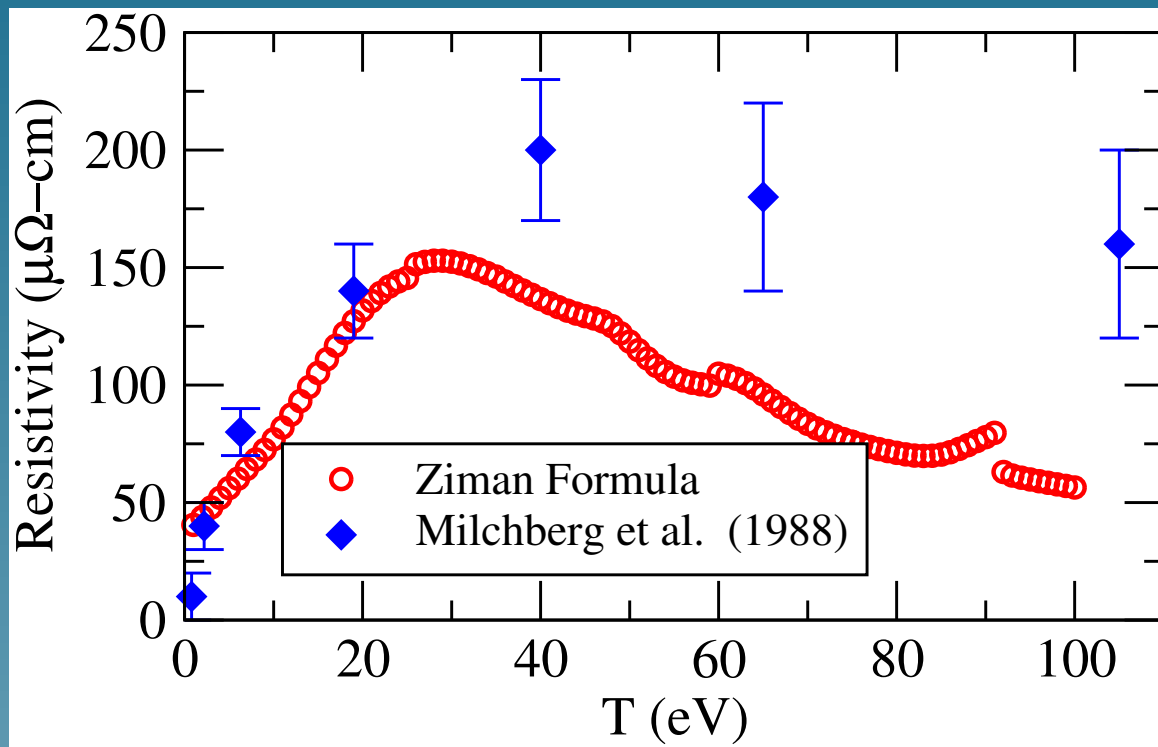
<sup>4</sup>G. D. Mahan, *Many-Particle Physics*, Plenum, 2000

## Phase Shifts



$T = 10$  eV and metallic density

## Resistivity of Aluminum



Metallic density

## Linear Response and the Kubo-Greenwood Formula

Apply an electric field to the average atom:

$$\mathbf{E}(t) = F \hat{z} \sin \omega t \quad \mathbf{A}(t) = \frac{F}{\omega} \hat{z} \cos \omega t$$

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The time dependent Schrödinger equation becomes

$$\left[ T_0 + V(n, r) - \frac{eF}{\omega} v_z \cos \omega t \right] \psi_i(\mathbf{r}, t) = i \frac{\partial}{\partial t} \psi_i(\mathbf{r}, t)$$

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The current density is

$$J_z(t) = \frac{2e}{\Omega} \sum_i f_i \langle \psi_i(t) | v_z | \psi_i(t) \rangle$$

## Solution Ansatz

$$\psi_i(\mathbf{r}, t) = u_i(\mathbf{r})e^{-i\epsilon_i t} + w_i^+(\mathbf{r})e^{-i(\epsilon_i + \omega)t} + w_i^-(\mathbf{r})e^{-i(\epsilon_i - \omega)t}$$

$$[T_0 + V(n, r)] u_i(\mathbf{r}) = \epsilon_i u_i(\mathbf{r})$$

$$[T_0 + V(n, r) - (\epsilon_i \pm \omega)] w_i^\pm(\mathbf{r}) = \frac{eF}{2\omega} v_z u_i(\mathbf{r})$$

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## Eigenvalue Expansion

$$w_i^+(\mathbf{r}) = \sum_j X_i^j u_j(\mathbf{r})$$

$$X_i^j = \frac{eF}{2\omega} \frac{\langle j|v_z|i\rangle}{\epsilon_j - i\eta - \epsilon_i - \omega}$$

$$w_i^-(\mathbf{r}) = \sum_j Y_i^j u_j(\mathbf{r})$$

$$Y_i^j = \frac{eF}{2\omega} \frac{\langle j|v_z|i\rangle}{\epsilon_j - i\eta - \epsilon_i + \omega}$$

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$$Y_i^j = \frac{eF}{2\omega} \frac{\langle j|v_z|i\rangle}{\epsilon_j - i\eta - \epsilon_i + \omega}$$

The response current may be written

$$\begin{aligned} J = \frac{4e}{\Omega} \sum_{ij} f_i & \left[ \Re \left( \langle i|v_z|j\rangle X_i^j + \langle j|v_z|i\rangle Y_i^{j*} \right) \cos \omega t \right. \\ & \left. + \Im \left( \langle i|v_z|j\rangle X_i^j + \langle j|v_z|i\rangle Y_i^{j*} \right) \sin \omega t \right] \end{aligned}$$

# Kubo-Greenwood

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Result:

$$\sigma(\omega) = \frac{2\pi e^2}{\omega\Omega} \sum_{ij} (f_i - f_j) |\langle j|v_z|i\rangle|^2 \delta(\epsilon_j - \epsilon_i - \omega),$$

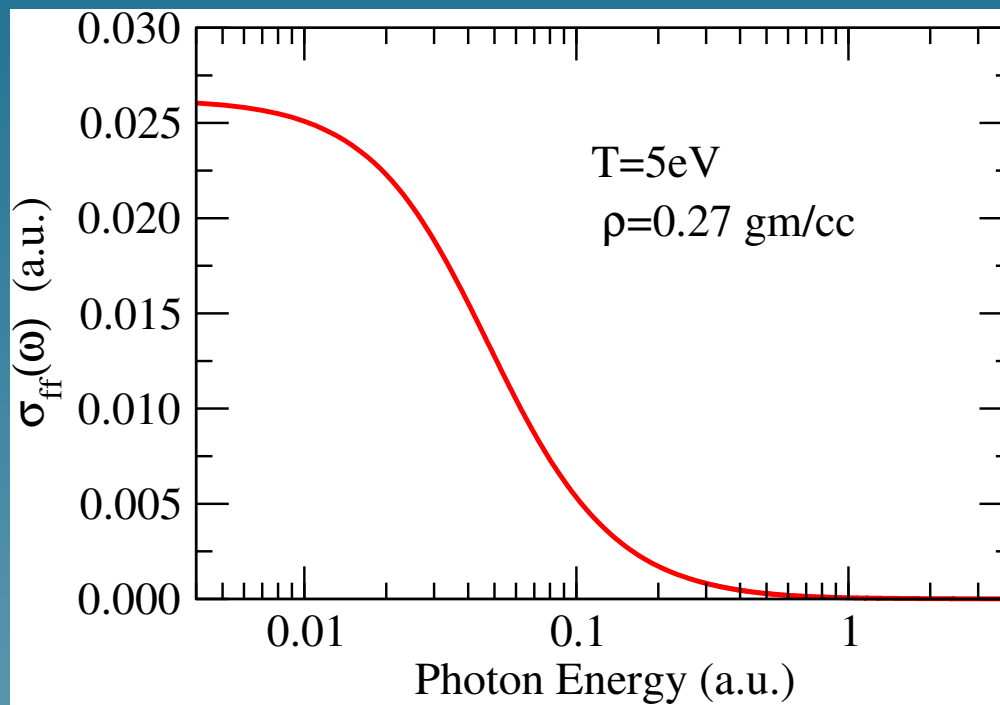
which is an average-atom version of the Kubo<sup>5</sup>-Greenwood<sup>6</sup> formula.

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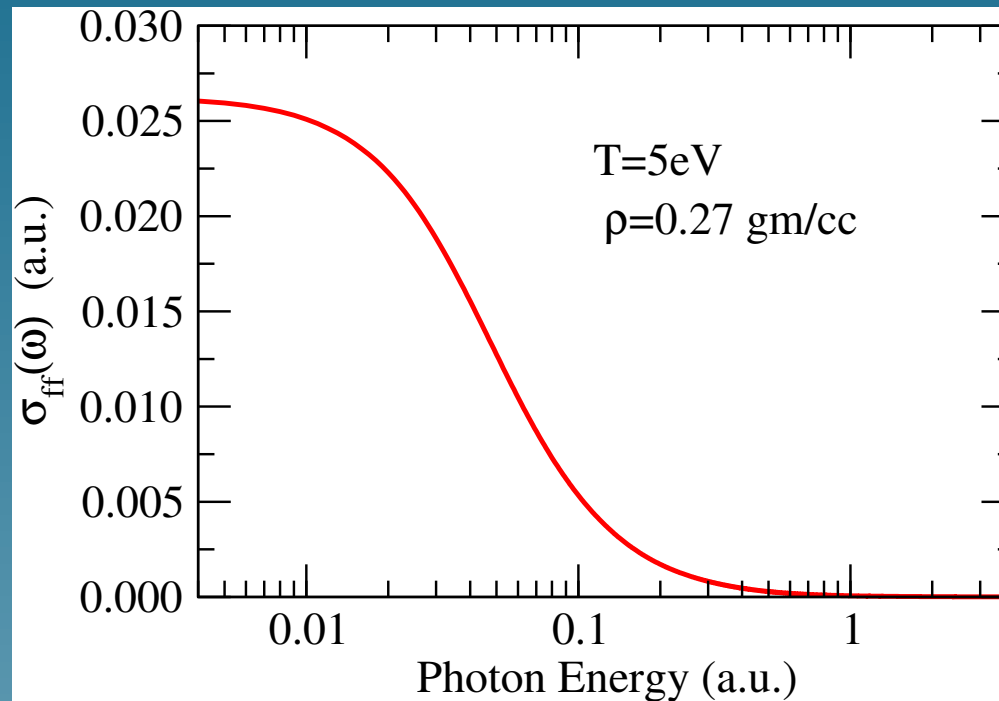
<sup>5</sup> R. Kubo, J. Phys. Soc. Jpn. **12**, 570 (1957)

<sup>6</sup>D. A. Greenwood, Proc. Phys. Soc. London **715**, 585 (1958)

## Free-Free Contribution to Conductivity

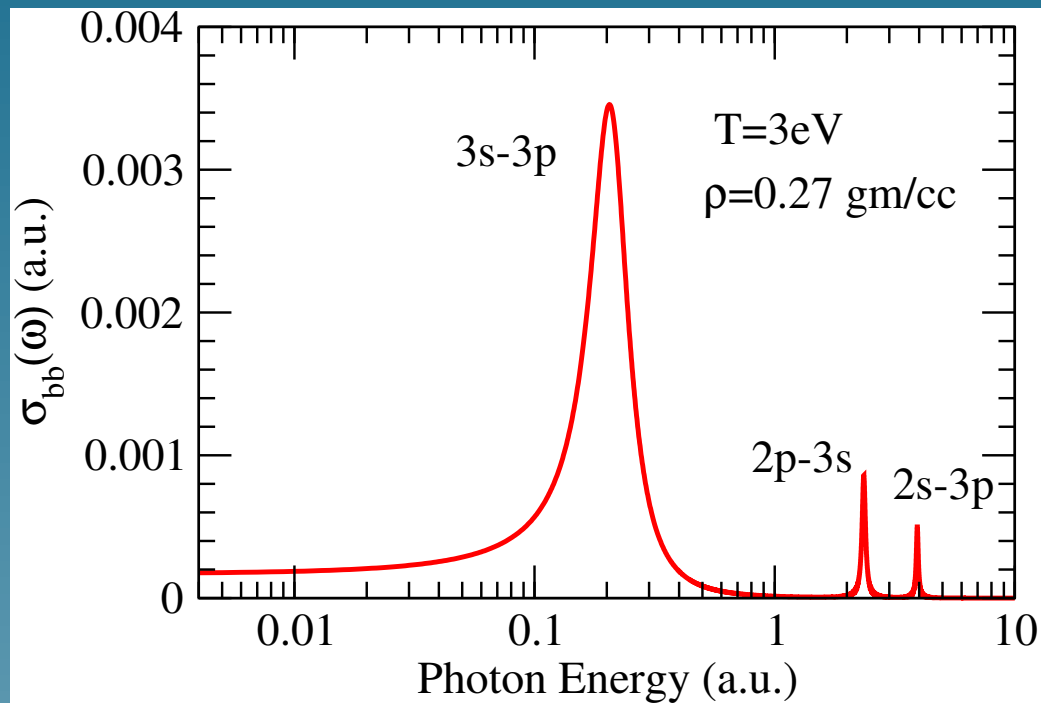


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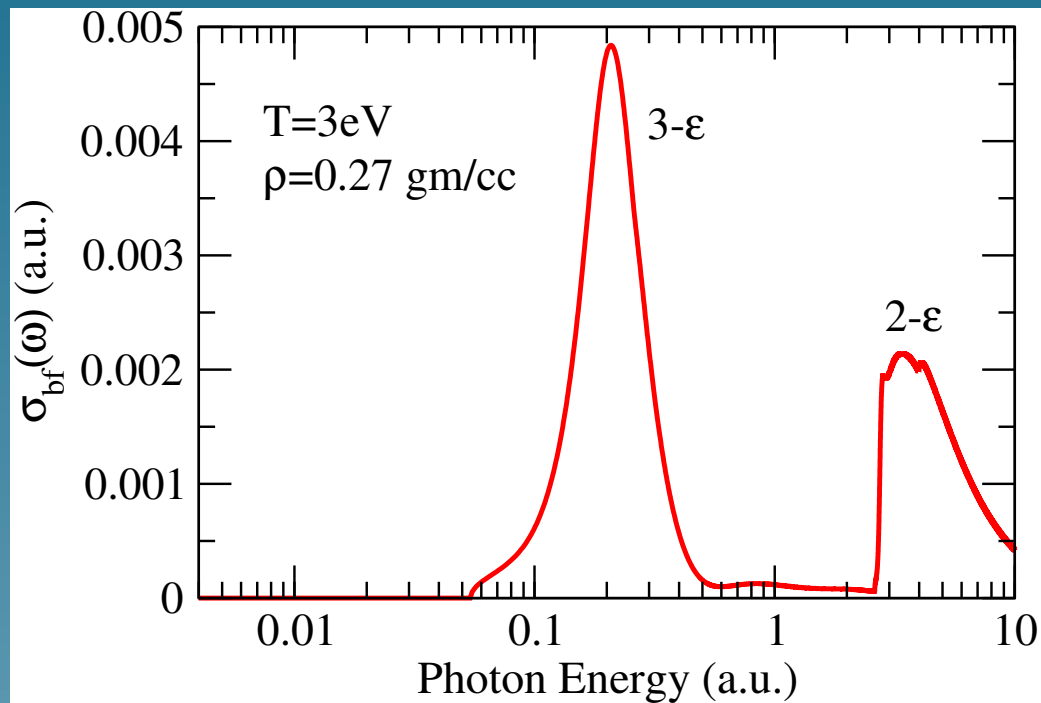


Michael Kuchiev has prepared an elegant note on the low-frequency conductivity explaining the origin of the infrared divergence and proposing a remedy.

## Bound-Bound Contribution to Conductivity



# Bound-Free Contribution to Conductivity



## Optical Properties

For a conducting medium, the dielectric function is related to the *complex* conductivity by

$$\epsilon(\omega) = 1 + 4\pi i \frac{\sigma(\omega)}{\omega}$$

We know  $\Re\sigma(\omega)$ ; we must evaluate  $\Im\sigma(\omega)$

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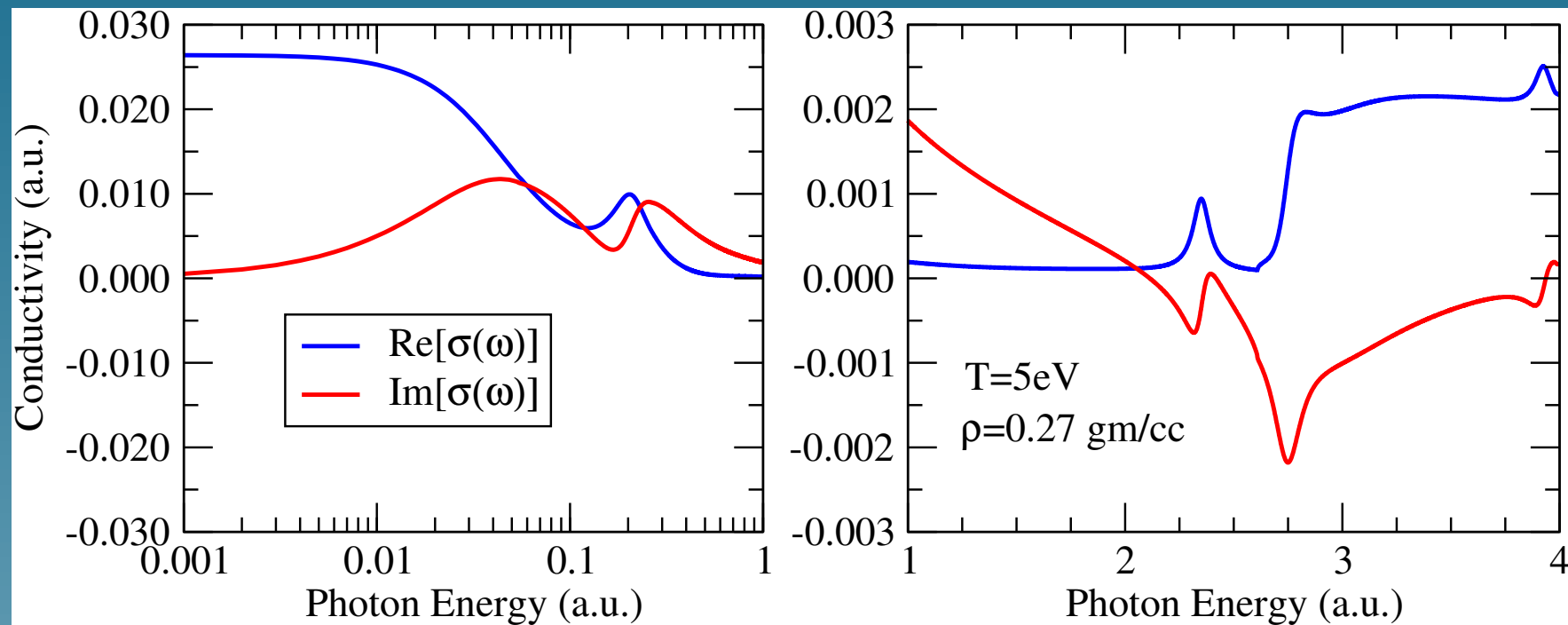
From analytic properties of  $\sigma(\omega)$  one infers the dispersion relation<sup>7</sup>

$$\Im\sigma(\omega_0) = \frac{2\omega_0}{\pi} \int_0^\infty \frac{\Re\sigma(\omega)}{\omega_0^2 - \omega^2} d\omega.$$

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<sup>7</sup>R. de L. Kronig and H. A. Kramers, Atti Congr. Intern. Fisici, **2**, 545 (1927)

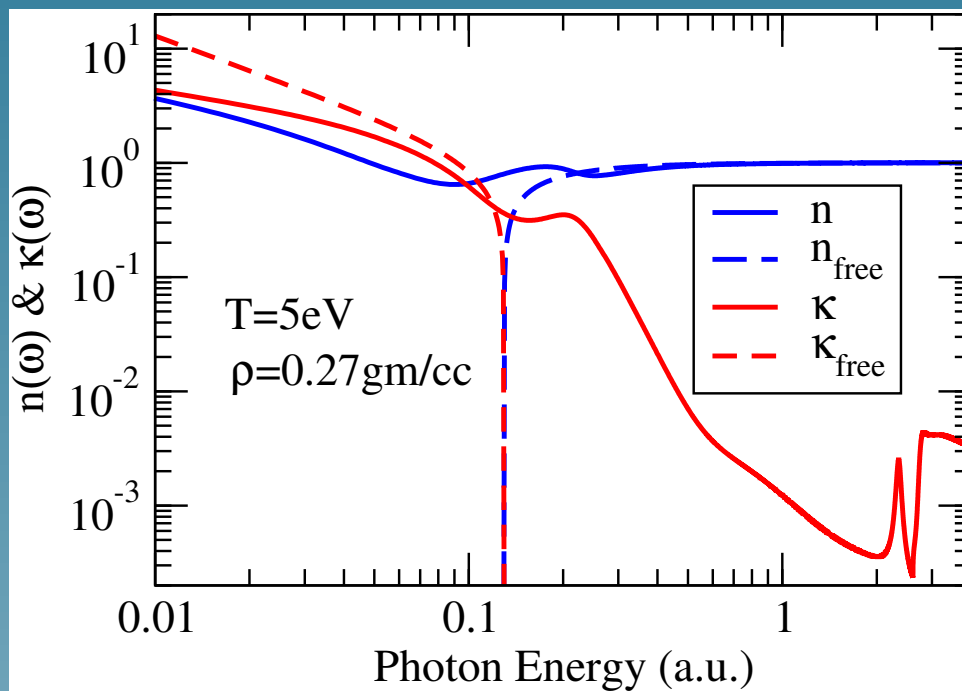
## Application of Dispersion Relation



## Index of Refraction

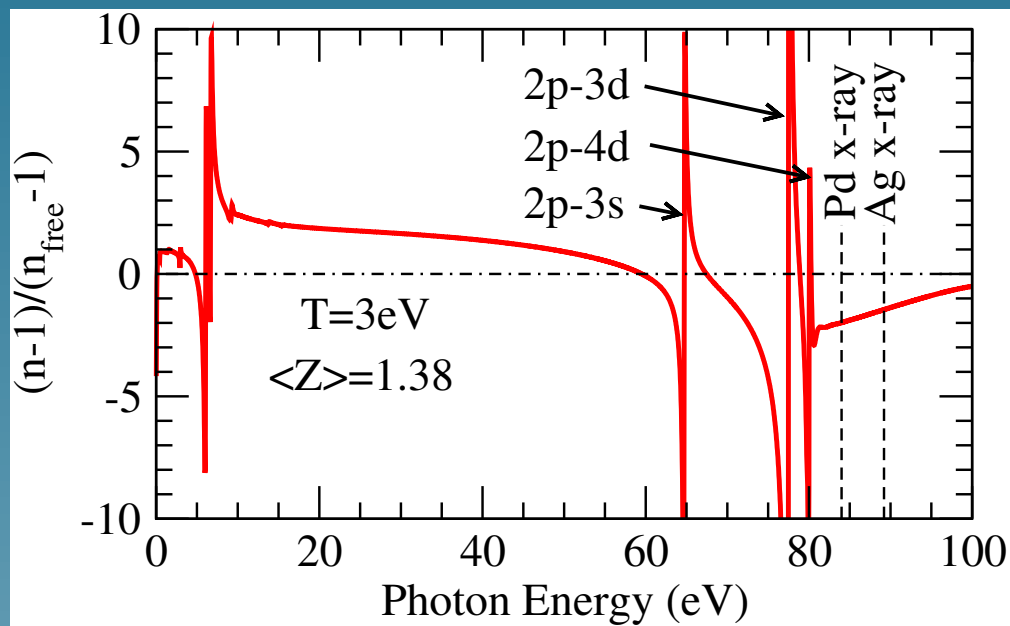
$$\Re\epsilon(\omega) = 1 - 4\pi \frac{\Im\sigma(\omega)}{\omega} \quad \Im\epsilon(\omega) = 4\pi \frac{\Re\sigma(\omega)}{\omega},$$

$$n + i\kappa = \sqrt{\epsilon}.$$



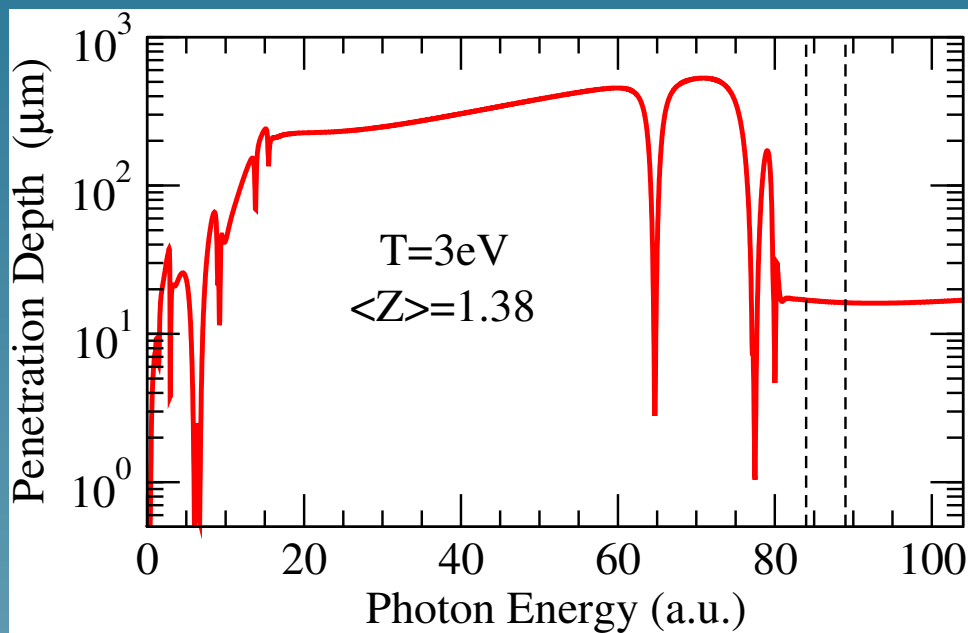
## Al: Comparison with Free Electron Model

Plasma with ion density  $n_{\text{ion}} = 10^{20}/\text{cc}$



## Al: Penetration Depth

Plasma with ion density  $n_{\text{ion}} = 10^{20}/\text{cc}$



## Conclusions

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- Average atom model is a simple way to understand the electronic structure of a plasma. (next step - look at neighbors)
- Linear response theory applied to the average atom model. provides a straightforward method for obtaining the frequency-dependent conductivity.
- The dielectric function (and index of refraction) can be reconstructed with the aid of a dispersion relation.
- The model explains “anomalous behavior” of low temperature Al plasmas in the 80-90 eV frequency range.

## Conclusions

- Average atom model is a simple way to understand the electronic structure of a plasma. (next step - look at neighbors)
- Linear response theory applied to the average atom model. provides a straightforward method for obtaining the frequency-dependent conductivity.
- The dielectric function (and index of refraction) can be reconstructed with the aid of a dispersion relation.
- The model explains “anomalous behavior” of low temperature Al plasmas in the 80-90 eV frequency range.

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