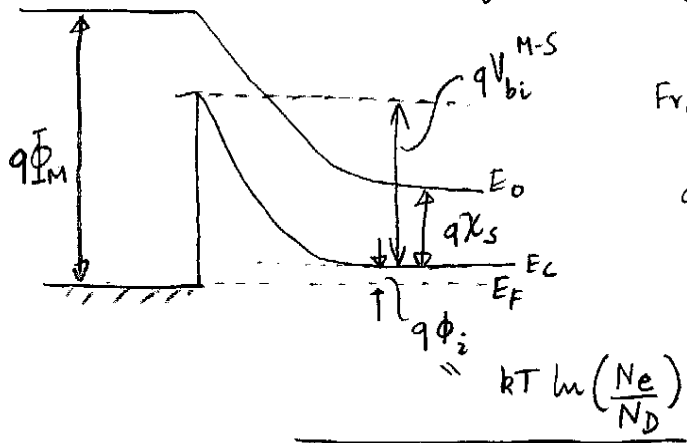


© STAEDTLER® No. 937 811E Engineer's Computation Pad

① Built-in voltage of the p-n junction:

$$V_{bi}^{p-n} = \frac{kT}{q} \ln\left(\frac{N_A N_D}{n_i^2}\right)$$



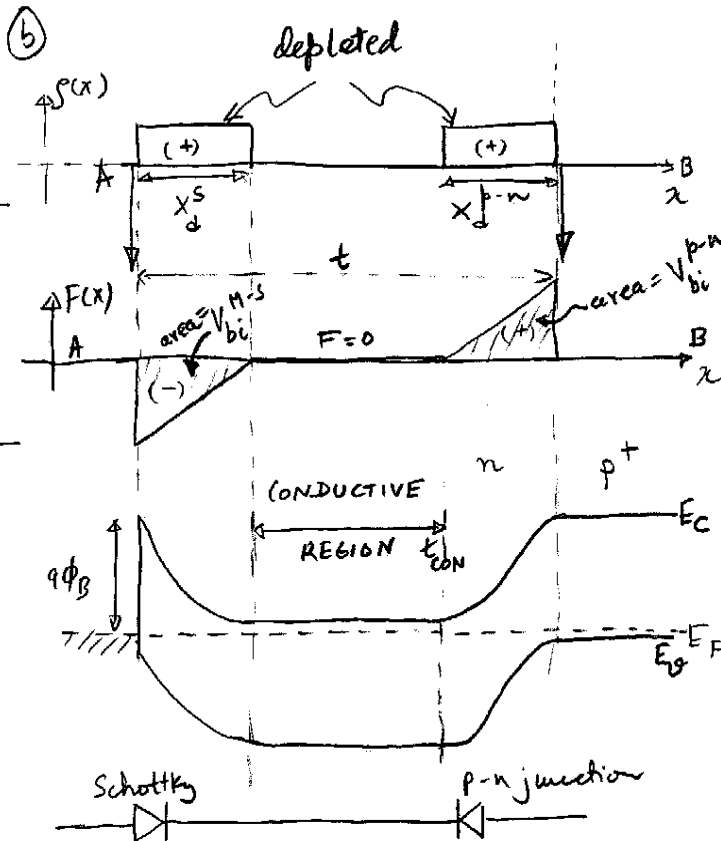
From band-diagram on left,

$$\begin{aligned} qV_{bi}^{M-S} &= q\Phi_M - q\chi_s - q\phi_i \\ &= q\Phi_M - q\chi_s - kT \ln\left(\frac{N_c}{N_D}\right) \\ &= qV_{bi}^{p-n} \text{ (Required)}. \end{aligned}$$

∴ The necessary work function is

$$\begin{aligned} q\Phi_M &= qV_{bi}^{p-n} + kT \ln\left(\frac{N_c}{N_D}\right) + q\chi_s \\ &= kT \ln\left(\frac{N_A N_D}{n_i^2}\right) + kT \ln\left(\frac{N_c}{N_D}\right) + q\chi_s \end{aligned}$$

$$q\Phi_M = q\chi_s + kT \ln\left(\frac{N_A N_c}{n_i^2}\right)$$



From the figure on left, the depletion widths of the M-S & p-n junctions are the SAME, since the voltage drops across them are the same!

$$\begin{aligned} x_d^S &= x_d^{p-n}, \text{ where} \\ V_{bi} &= \frac{qN_D x_d^2}{2\epsilon_s} \quad @ V_g = 0. \end{aligned}$$

$$x_d^S = x_d^{p-n} = \sqrt{\frac{2\epsilon_s V_{bi}}{qN_D}}$$

∴ The conductive region thickness is

$$t_{con} = t - 2x_d^S = t - 2\sqrt{\frac{2\epsilon_s V_{bi}}{qN_D}}$$

Obviously, $t \geq \frac{8\epsilon_s V_{bi}}{qN_D}$

Contd...

(c) Since the Schottky contact to n-layer & the ohmic contact to the p-layer are at the same potential,

$\left. \begin{array}{l} \text{+ve } V_g \Rightarrow \text{ Depletion layer thicknesses } x_d^S \text{ \& } x_d^{p-n} \text{ shrink, n-layer} \\ \text{more conductive.} \\ \text{-ve } V_g \Rightarrow \text{ Depletion layer thicknesses } x_d^S \text{ \& } x_d^{p-n} \text{ stretch, n-layer} \\ \text{less conductive.} \end{array} \right\}$

It is clear that a -ve V_g is needed to deplete the n-layer
When a bias is applied,

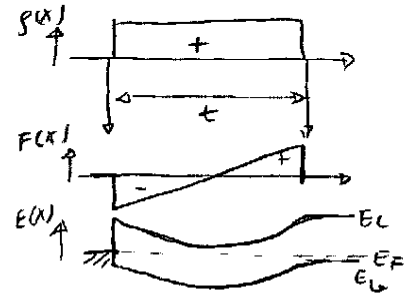
$$x_d^S = \sqrt{\frac{2\epsilon_s (V_{bi} + |V_g|)}{qN_D}}$$

$$x_d^{p-n} \approx \sqrt{\frac{2\epsilon_s (V_{bi} + |V_g|)}{qN_D}}$$

$$\therefore t_{con} = t - \left\{ \sqrt{\frac{2\epsilon_s (V_{bi} + |V_g|)}{qN_D}} + \sqrt{\frac{2\epsilon_s (V_{bi} + |V_g|)}{qN_D}} \right\} \left(\frac{1}{N_A} + \frac{1}{N_D} \right) = \frac{t}{N_D} \text{ since } N_A \gg N_D$$

(c) pinch-off, $t_{con} = 0 \Rightarrow$

$$t = 2 \sqrt{\frac{2\epsilon_s (V_{bi} + |V_g|)}{qN_D}}$$



$$\Rightarrow V_g(\text{pinch-off}) = \frac{qN_D}{8\epsilon_s} t^2 - V_{bi}$$

