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# EE566 Solid State Devices

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## Assignment 4

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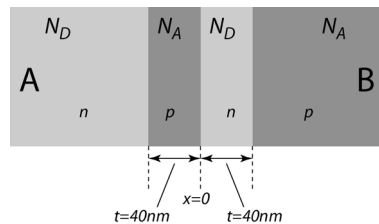
**Reading:** Chapter 2 from Shur

*p-n junction currents: The long, the short, and the funny*

### Problem 1: The Funny Junction

Consider the silicon p-n junction shown below with a rather messed-up junction region.

- Sketch the charge, electric field and band diagram for this device at zero applied bias. What is the built-in voltage between the quasi-neutral regions in A and B? Use  $n_i=6.68 \times 10^9/cm^3$ , and  $N_D=N_A=10^{17}/cm^3$ . Assume regions A and B to be very long.
- Find a *general algebraic relation* between the depletion widths  $W$  in regions A and B in terms of the thickness  $t$  and the built-in voltage  $V_{bi}$ . Do NOT neglect Gummel correction. Assume  $N_D=N_A=N_o$  for simplicity. Then, calculate  $W$  for  $t=40nm$ ,  $N_o=10^{17}/cm^3$ .
- At what bias voltage will the electric field at  $x=0$  fall to zero? Find algebraically first, then calculate the numerical value. Is it forward-bias or reverse-bias?
- At this bias, sketch the band diagram, showing the quasi-Fermi levels.
- Find the total current density (in  $A/cm^2$ ) flowing through our funny junction at this bias. Use  $\tau_n=\tau_p=10\mu s$ .



### Problem 2: Long and Short p-n junction currents

We will henceforth call the heavily doped side of an asymmetrical p-n junction as the *EMITTER*, and the lightly doped side the *BASE*, to prepare for the jargon used in bipolar transistors. Consider an ideal  $n^+-p$  junction made of silicon ( $N_D=10^{17}/cm^3$ ,  $N_A=10^{15}/cm^3$ ) at 300K. Assume that the minority carrier lifetime of electrons in the p-side and holes in the n-side is  $\tau_n=\tau_p=0.1\mu s$ . Look up data sheets for anything else you might need.

- Calculate the saturation current density  $J_0$  for the diode (current density is  $J=J_0[\exp(V/V_{th})-1]$ ).
- Sketch the minority and majority carrier profiles outside the depletion region at zero bias, and at a forward bias of  $V=0.5$  Volt. Label length scales (diffusion lengths, etc).
- Calculate and sketch the electron and hole current components (both diffusion and recombination) outside the depletion region as a function of distance at this forward bias. Which carriers (minority or majority) dominate the current flow on each side of the junction?
- Redo parts a) to c) for a *short-base* diode, with the *total* base width (thickness of the p-side)  $W_B=2\mu m$ . Verify that  $W_B \ll L_n$ , where  $L_n$  is the minority carrier diffusion length in the base. Make reasonable approximations (linearize slow exponentials, etc) to simplify the problem.
- Finally, what we were waiting for – when is the current larger – for long base or short base? Can you explain intuitively why this must be so?