# Continuous uniform probability model 

Math 30530, Fall 2013

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(4) Consequence: If $p$ is a particular point in $R$, then (homework!)

$$
\operatorname{Pr}(p)=0
$$

This is an example of an event that could occur, but has probability 0 of occurring

