The basic elements of probability

Math 30530, Fall 2013

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Math 30530 (Fall 2012)

Probability basics

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 $Pr(\Omega) = 1$