## A puzzler about a chessboard

How many rectangles are there on an ordinary chess board?


Three possibilities are shown on the picture above

## Answer

A rectangle is determined by the consecutive collection of squares it spans horizontally, and the collection of squares it spans vertically
There are 8 possibilities for a horizontal span of one square, 7 for a horizontal span of two squares, 6 for three squares, 5 for four, 4 for five, 3 for six, 2 for seven, and one possibility for a horizontal span of eight squares, for a total of $8+7+6+5+4+3+2+1=36$ possibilities for the horizontal span.
Similarly there are 36 possibilities for the horizontal span.
This leads to $36 \times 36=1296$ different rectangles.

